Model Predictive Control Toolbox™ Getting Started Guide

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Model Predictive Control Toolbox[™] Getting Started Guide

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Introduction

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Model Predictive Control Toolbox Product Description Design and simulate model predictive controllers

Model Predictive Control Toolbox provides functions, an app, and Simulink[®] blocks for designing and simulating model predictive controllers (MPCs). The toolbox lets you specify plant and disturbance models, horizons, constraints, and weights. By running closed-loop simulations, you can evaluate controller performance.

You can adjust the behavior of the controller by varying its weights and constraints at run time. To control a nonlinear plant, you can implement adaptive and gain-scheduled MPCs. For applications with fast sample rates, you can generate an explicit model predictive controller from a regular controller or implement an approximate solution.

For rapid prototyping and embedded system implementation, the toolbox supports automatic C-code and IEC 61131-3 Structured Text generation.

Key Features

- App for interactive design of MPC controllers
- Runtime adjustment of weights and constraints
- Adaptive and gain-scheduled MPCs for controlling systems with nonlinear dynamics
- Explicit MPC and approximate solution for guaranteed worst-case execution time
- Economic MPC with arbitrary nonlinear cost function and constraints
- Computationally efficient quadratic programming (QP) solver, and support for third-party solvers
- Support for C-code generation (with Simulink Coder[™]) and IEC 61131-3 Structured Text generation (with Simulink PLC Coder[™])

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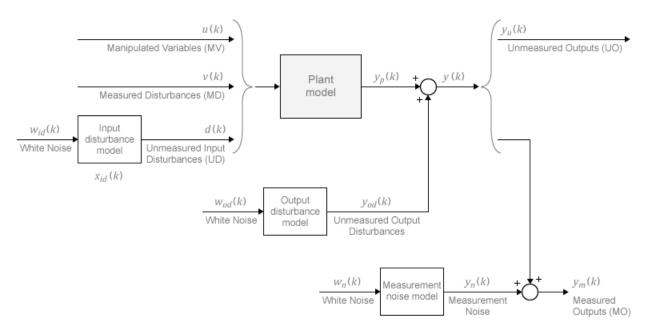
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Building Models

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MPC Modeling

Model predictive controllers use plant, disturbance, and noise models for prediction and state estimation. The model structure used in an MPC controller appears in the following illustration.



Plant Model

You can specify the plant model in one of the following linear-time-invariant (LTI) formats:

- Numeric LTI models Transfer function (tf), state space (ss), zero-pole-gain (zpk)
- Identified models (requires System Identification Toolbox[™]) idss, idtf, idproc, and idpoly

The MPC controller performs all estimation and optimization calculations using a discrete-time, delay-free, state-space system with dimensionless input and output variables. Therefore, when you specify a plant model in the MPC controller, the software performs the following, if needed:

- **1** Conversion to state space The **ss** command converts the supplied model to an LTI state-space model.
- **2** Discretization or resampling If the model sample time differs from the MPC controller sample time (defined in the Ts property), one of the following occurs:
 - If the model is continuous time, the c2d command converts it to a discrete-time LTI object using the controller sample time.
 - If the model is discrete time, the d2d command resamples it to generate a discrete-time LTI object using the controller sample time.
- 3 Delay removal If the discrete-time model includes any input, output, or internal delays, the absorbDelay command replaces them with the appropriate number of poles at z = 0, increasing the total number of discrete states. The InputDelay, OutputDelay, and InternalDelay properties of the resulting state space model are all zero.
- 4 Conversion to dimensionless input and output variables The MPC controller enables you to specify a scale factor for each plant input and output variable. If you do not specify scale factors, they default to 1. The software converts the plant input and output variables to dimensionless form as follows:

$$x_p(k+1) = A_p x_p(k) + BS_i u_p(k)$$
$$y_p(k) = S_0^{-1} C x_p(k) + S_0^{-1} DS_i u_p(k) .$$

where A_p , B, C, and D are the constant state-space matrices determined in step 3, and:

- S_i is a diagonal matrix of input scale factors in engineering units.
- S_o is a diagonal matrix of output scale factors in engineering units.
- x_p is the state vector from step 3 in engineering units. No scaling is performed on state variables.
- u_p is a vector of dimensionless plant input variables.
- y_p is a vector of dimensionless plant output variables.

The resulting plant model has the following equivalent form:

$$\begin{split} x_p(k+1) &= A_p x_p(k) + B_{pu} u(k) + B_{pv} v(k) + B_{pd} d(k) \\ y_p(k) &= C_p x_p(k) + D_{pu} u(k) + D_{pv} v(k) + D_{pd} d(k) \,. \end{split}$$

Here, $C_p = S_o^{-1}C$, B_{pu} , B_{pv} , and B_{pd} are the corresponding columns of BS_i . Also, D_{pu} , D_{pv} , and D_{pd} are the corresponding columns of $S_o^{-1}DS_i$. Finally, u(k), v(k), and d(k) are the dimensionless manipulated variables, measured disturbances, and unmeasured input disturbances, respectively.

The MPC controller enforces the restriction of $D_{pu} = 0$, which means that the controller does not allow direct feedthrough from any manipulated variable to any plant output.

Input Disturbance Model

If your plant model includes unmeasured input disturbances, d(k), the input disturbance model specifies the signal type and characteristics of d(k). See "Controller State Estimation" for more information about the model.

The getindist command provides access to the model in use.

The input disturbance model is a key factor that influences the following controller performance attributes:

- Dynamic response to apparent disturbances The character of the controller response when the measured plant output deviates from its predicted trajectory, due to an unknown disturbance or modeling error.
- Asymptotic rejection of sustained disturbances If the disturbance model predicts a sustained disturbance, controller adjustments continue until the plant output returns to its desired trajectory, emulating a classical integral feedback controller.

You can provide the input disturbance model as an LTI state-space (ss), transfer function (tf), or zero-pole-gain (zpk) object using setindist. The MPC controller converts the input disturbance model to a discrete-time, delay-free, LTI state-space system using the same steps used to convert the plant model on page 2-2. The result is:

$$\begin{aligned} x_{id}(k+1) &= A_{id}x_{id}(k) + B_{id}w_{id}(k) \\ d(k) &= C_{id}x_{id}(k) + D_{id}w_{id}(k) \,. \end{aligned}$$

where A_{id} , B_{id} , C_{id} , and D_{id} are constant state-space matrices, and:

• $x_{id}(k)$ is a vector of $n_{xid} \ge 0$ input disturbance model states.

- $d_k(k)$ is a vector of n_d dimensionless unmeasured input disturbances.
- $w_{id}(k)$ is a vector of $n_{id} \ge 1$ dimensionless white noise inputs, assumed to have zero mean and unit variance.

If you do not provide an input disturbance model, then the controller uses a default model, which has integrators with dimensionless unity gain added to its outputs. An integrator is added for each unmeasured input disturbance, unless doing so would cause a violation of state observability. In this case, a static system with dimensionless unity gain is used instead.

Output Disturbance Model

The output disturbance model is a special case of the more general input disturbance model. Its output, $y_{od}(k)$, is directly added to the plant output rather than affecting the plant states. The output disturbance model specifies the signal type and characteristics of $y_{od}(k)$, and it is often used in practice. See "Controller State Estimation" for more details about the model.

The getoutdist command provides access to the output disturbance model in use.

You can specify a custom output disturbance model as an LTI state-space (ss), transfer function (tf), or zero-pole-gain (zpk) object using setoutdist. Using the same steps as for the plant model on page 2-2, the MPC controller converts the specified output disturbance model to a discrete-time, delay-free, LTI state-space system. The result is:

$$\begin{aligned} x_{od}(k+1) &= A_{od} x_{od}(k) + B_{od} w_{od}(k) \\ y_{od}(k) &= C_{od} x_{od}(k) + D_{od} w_{od}(k) \,. \end{aligned}$$

where A_{od} , B_{od} , C_{od} , and D_{od} are constant state-space matrices, and:

- $x_{od}(k)$ is a vector of $n_{xod} \ge 1$ output disturbance model states.
- $y_{od}(k)$ is a vector of n_y dimensionless output disturbances to be added to the dimensionless plant outputs.
- $w_{od}(k)$ is a vector of n_{od} dimensionless white noise inputs, assumed to have zero mean and unit variance.

If you do not specify an output disturbance model, then the controller uses a default model, which has integrators with dimensionless unity gain added to some or all of its outputs. These integrators are added according to the following rules:

- No disturbances are estimated, that is no integrators are added, for unmeasured plant outputs.
- An integrator is added for each measured output in order of decreasing output weight.
 - For time-varying weights, the sum of the absolute values over time is considered for each output channel.
 - For equal output weights, the order within the output vector is followed.
- For each measured output, an integrator is not added if doing so would cause a violation of state observability. Instead, a gain with a value of zero is used instead.

If there is an input disturbance model, then the controller adds any default integrators to that model before constructing the default output disturbance model.

Measurement Noise Model

One controller design objective is to distinguish disturbances, which require a response, from measurement noise, which should be ignored. The measurement noise model specifies the expected noise type and characteristics. See "Controller State Estimation" for more details about the model.

Using the same steps as for the plant model on page 2-2, the MPC controller converts the measurement noise model to a discrete-time, delay-free, LTI state-space system. The result is:

$$\begin{aligned} x_n(k+1) &= A_n x_n(k) + B_n w_n(k) \\ y_n(k) &= C_n x_n(k) + D_n w_n(k) \,. \end{aligned}$$

Here, A_n , B_n , C_n , and D_n are constant state space matrices, and:

- $x_n(k)$ is a vector of $n_{xn} \ge 0$ noise model states.
- $y_n(k)$ is a vector of n_{ym} dimensionless noise signals to be added to the dimensionless measured plant outputs.
- $w_n(k)$ is a vector of $n_n \ge 1$ dimensionless white noise inputs, assumed to have zero mean and unit variance.

If you do not supply a noise model, the default is a unity static gain: $n_{xn} = 0$, D_n is an n_{ym} -by- n_{ym} identity matrix, and A_n , B_n , and C_n are empty.

For an mpc controller object, MPCobj, the property MPCobj.Model.Noise provides access to the measurement noise model.

Note If the minimum eigenvalue of $D_n D_n^T$ is less than 1×10^{-8} , the MPC controller adds 1×10^{-4} to each diagonal element of D_n . This adjustment makes a successful default Kalman gain calculation more likely.

See Also

More About

• "Controller State Estimation"

Signal Types

Inputs

The *plant inputs* are the independent variables affecting the plant. As shown in "MPC Modeling" on page 2-2, there are three types:

Measured disturbances

The controller can't adjust them, but uses them for feedforward compensation.

Manipulated variables

The controller adjusts these in order to achieve its goals.

Unmeasured disturbances

These are independent inputs of which the controller has no direct knowledge, and for which it must compensate.

Outputs

The *plant outputs* are the dependent variables (outcomes) you wish to control or monitor. As shown in "MPC Modeling" on page 2-2, there are two types:

Measured outputs

The controller uses these to estimate unmeasured quantities and as feedback on the success of its adjustments.

Unmeasured outputs

The controller estimates these based on available measurements and the plant model. The controller can also hold unmeasured outputs at setpoints or within constraint boundaries.

You must specify the input and output types when designing the controller. See "Input and Output Types" on page 2-14 for more details.

See Also

More About

• "MPC Modeling" on page 2-2

Construct Linear Time Invariant (LTI) Models

Model Predictive Control Toolbox software supports the same LTI model formats as does Control System Toolbox software. You can use whichever is most convenient for your application. It's also easy to convert from one format to another. For more details, see the Control System Toolbox documentation.

Transfer Function Models

A transfer function (TF) relates a particular input/output pair. For example, if u(t) is a plant input and y(t) is an output, the transfer function relating them might be:

$$\frac{Y(s)}{U(s)} = G(s) = \frac{s+2}{s^2+s+10}e^{-1.5s}$$

This TF consists of a *numerator* polynomial, s+2, a *denominator* polynomial, s^2+s+10 , and a delay, which is 1.5 time units here. You can define G using Control System Toolbox tf function:

Gtf1 = tf([1 2], [1 1 10], 'OutputDelay', 1.5)

Control System Toolbox software builds and displays it as follows:

Zero/Pole/Gain Models

Like the TF, the zero/pole/gain (ZPK) format relates an input/output pair. The difference is that the ZPK numerator and denominator polynomials are factored, as in

 $G(s) = 2.5 \frac{s + 0.45}{(s + 0.3)(s + 0.1 + 0.7i)(s + 0.1 - 0.7i)}$

(zeros and/or poles are complex numbers in general).

You define the ZPK model by specifying the zero(s), pole(s), and gain as in

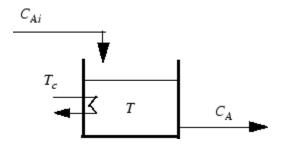
poles = [-0.3, -0.1+0.7*i, -0.1-0.7*i]; Gzpk1 = zpk(-0.45,poles,2.5);

State-Space Models

The state-space format is convenient if your model is a set of LTI differential and algebraic equations. For example, consider the following linearized model of a continuous stirred-tank reactor (CSTR) involving an exothermic (heat-generating) reaction [1].

$$\frac{dC'_A}{dt} = a_{11}C'_A + a_{12}T' + b_{11}T'_c + b_{12}C'_{Ai}$$
$$\frac{dT'}{dt} = a_{21}C'_A + a_{22}T' + b_{21}T'_c + b_{22}C'_{Ai}$$

where C_A is the concentration of a key reactant, T is the temperature in the reactor, T_c is the coolant temperature, C_{Ai} is the reactant concentration in the reactor feed, and a_{ij} and b_{ij} are constants. See the process schematic in "CSTR Schematic" on page 2-11. The primes (e.g., C_A) denote a deviation from the nominal steady-state condition at which the model has been linearized.



CSTR Schematic

Measurement of reactant concentrations is often difficult, if not impossible. Let us assume that T is a measured output, C_A is an unmeasured output, T_c is a manipulated variable, and C_{Ai} is an unmeasured disturbance.

The model fits the general state-space format

$$\frac{dx}{dt} = Ax + Bu$$
$$y = Cx + Du$$

where

$$x = \begin{bmatrix} C'_{A} \\ T' \end{bmatrix}, u = \begin{bmatrix} T'_{C} \\ C'_{Ai} \end{bmatrix}, y = \begin{bmatrix} T' \\ C'_{A} \end{bmatrix}$$
$$A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}, B = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix}, C = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}, D = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

The following code shows how to define such a model for some specific values of the a_{ij} and b_{ij} constants:

```
A = [-0.0285 -0.0014

-0.0371 -0.1476];

B = [-0.0850 0.0238

0.0802 0.4462];

C = [0 1

1 0];

D = zeros(2,2);

CSTR = ss(A,B,C,D);
```

This defines a *continuous-time* state-space model. If you do not specify a sampling period, a default sampling value of zero applies. You can also specify discrete-time state-space models. You can specify delays in both continuous-time and discrete-time models.

Note In the CSTR example, the *D* matrix is zero and the output does not instantly respond to change in the input. The Model Predictive Control Toolbox software prohibits direct (instantaneous) feedthrough from a manipulated variable to an output. For example, the CSTR model could include direct feedthrough from the unmeasured disturbance, C_{Ai} , to either C_A or *T* but direct feedthrough from T_c to either output would violate this restriction. If the model had direct feedthrough from T_c , you can add a small delay at this input to circumvent the problem.

LTI Object Properties

The ss function in the last line of the above code creates a state-space model, CSTR, which is an *LTI object*. The tf and zpk commands described in "Transfer Function Models" on page 2-10 and "Zero/Pole/Gain Models" on page 2-10 also create LTI objects. Such objects contain the model parameters as well as optional properties.

LTI Properties for the CSTR Example

The following code sets some of the CSTR model's optional properties:

```
CSTR.InputName = { 'T_c', 'C_A_i'};
CSTR.OutputName = { 'T', 'C_A'};
CSTR.StateName = { 'C_A', 'T'};
CSTR.InputGroup.MV = 1;
CSTR.InputGroup.UD = 2;
CSTR.OutputGroup.UO = 1;
CSTR.OutputGroup.UO = 2;
CSTR
```

The first three lines specify labels for the input, output and state variables. The next four specify the signal type for each input and output. The designations MV, UD, MO, and UO mean *manipulated variable*, *unmeasured disturbance*, *measured output*, and *unmeasured output*. (See "Signal Types" on page 2-8 for definitions.) For example, the code specifies that input 2 of model CSTR is an unmeasured disturbance. The last line causes the LTI object to be displayed, generating the following lines in the MATLAB® Command Window:

A =СA Т C A -0.0285 -0.0014 Т -0.0371 -0.1476 B = Τс C Ai C A -0.085 0.0238 0.0802 0.4462 Т C = СА Т Т 0 1 C A 1 0 D = Тс САі 0 0 Т C A 0 0 Input groups: Name Channels MV 1 2 UD Output groups: Name Channels

M0 1 U0 2

Continuous-time model

Input and Output Names

The optional InputName and OutputName properties affect the model displays, as in the above example. The software also uses the InputName and OutputName properties to label plots and tables. In that context, the underscore character causes the next character to be displayed as a subscript.

Input and Output Types

General Case

As mentioned in "Signal Types" on page 2-8, Model Predictive Control Toolbox software supports three input types and two output types. In a Model Predictive Control Toolbox design, designation of the input and output types determines the controller dimensions and has other important consequences.

For example, suppose your plant structure were as follows:

Plant Inputs	Plant Outputs
Two manipulated variables (MVs)	Three measured outputs (MOs)
One measured disturbance (MD)	Two unmeasured outputs (UOs)
Two unmeasured disturbances (UDs)	

The resulting controller has four inputs (the three MOs and the MD) and two outputs (the MVs). It includes feedforward compensation for the measured disturbance, and assumes that you wanted to include the unmeasured disturbances and outputs as part of the regulator design.

If you didn't want a particular signal to be treated as one of the above types, you could do one of the following:

- Eliminate the signal before using the model in controller design.
- For an output, designate it as unmeasured, then set its weight to zero.
- For an input, designate it as an unmeasured disturbance, then define a custom state estimator that ignores the input.

Note By default, the software assumes that unspecified plant inputs are manipulated variables, and unspecified outputs are measured. Thus, if you didn't specify signal types in the above example, the controller would have four inputs (assuming all plant outputs were measured) and five outputs (assuming all plant inputs were manipulated variables).

For model CSTR, the default Model Predictive Control Toolbox assumptions are incorrect. You must set its InputGroup and OutputGroup properties, as illustrated in the above code, or modify the default settings when you load the model into **MPC Designer**.

Use **setmpcsignals** to make type definition. For example:

```
CSTR = setmpcsignals(CSTR, 'UD', 2, 'UO', 2);
```

sets InputGroup and OutputGroup to the same values as in the previous example. The CSTR display would then include the following lines:

Input groups: Name	Channels
Unmeasured	2
Manipulated	1
Output groups:	
Name	Channels
Unmeasured	2
Measured	1

Notice that setmpcsignals sets unspecified inputs to Manipulated and unspecified outputs to Measured.

LTI Model Characteristics

Control System Toolbox software provides functions for analyzing LTI models. Some of the more commonly used are listed below. Type the example code at the MATLAB prompt to see how they work for the CSTR example.

Example	Intended Result
-	Calculate gain matrix for the CSTR model's input/output pairs.

Example	Intended Result
<pre>impulse(CSTR)</pre>	Graph CSTR model's unit-impulse response.
linearSystemAnalyzer(CSTR)	Open the Linear System Analyzer with the CSTR model loaded. You can then display model characteristics by making menu selections.
pole(CSTR)	Calculate CSTR model's poles (to check stability, etc.).
<pre>step(CSTR)</pre>	Graph CSTR model's unit-step response.
zero(CSTR)	Compute CSTR model's transmission zeros.

References

[1] Seborg, D. E., T. F. Edgar, and D. A. Mellichamp, Process Dynamics and Control, 2nd Edition, Wiley, 2004, pp. 34-36 and 94-95.

See Also

 $\verb+setmpcsignals|ss|tf|zpk+$

More About

• "Specify Multi-Input Multi-Output Plants" on page 2-17

Specify Multi-Input Multi-Output Plants

Most MPC applications involve plants with multiple inputs and outputs. You can use ss, tf, and zpk to represent a MIMO plant model. For example, consider the following model of a distillation column [1], which has been used in many advanced control studies:

$$\begin{bmatrix} y_1 \\ y_2 \end{bmatrix} = \begin{bmatrix} \frac{12.8e^{-s}}{16.7s+1} & \frac{-18.9e^{-3s}}{21.0s+1} & \frac{3.8e^{-8.1s}}{14.9s+1} \\ \frac{6.6e^{-7s}}{10.9s+1} & \frac{-19.4e^{-3s}}{14.4s+1} & \frac{4.9e^{-3.4s}}{13.2s+1} \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \\ u_3 \end{bmatrix}$$

Outputs y_1 and y_2 represent measured product purities. The controller manipulates the inputs, u_1 and u_2 , to hold each output at a specified setpoint. These inputs represent the flow rates of reflux and reboiler steam, respectively. Input u_3 is a measured feed flow rate disturbance.

The model consists of six transfer functions, one for each input/output pair. Each transfer function is the first-order-plus-delay form often used by process control engineers.

Specify the individual transfer functions for each input/output pair. For example, g12 is the transfer function from input u_1 to output y_2 .

```
g11 = tf( 12.8, [16.7 1], 'IOdelay', 1.0, 'TimeUnit', 'minutes');
g12 = tf(-18.9, [21.0 1], 'IOdelay', 3.0, 'TimeUnit', 'minutes');
g13 = tf( 3.8, [14.9 1], 'IOdelay', 8.1, 'TimeUnit', 'minutes');
g21 = tf( 6.6, [10.9 1], 'IOdelay', 7.0, 'TimeUnit', 'minutes');
g22 = tf(-19.4, [14.4 1], 'IOdelay', 3.0, 'TimeUnit', 'minutes');
g23 = tf( 4.9, [13.2 1], 'IOdelay', 3.4, 'TimeUnit', 'minutes');
```

Define a MIMO system by creating a matrix of transfer function models.

DC = [g11 g12 g13 g21 g22 g23];

Define the input and output signal names and specify the third input as a measured input disturbance.

```
DC.InputName = {'Reflux Rate', 'Steam Rate', 'Feed Rate'};
DC.OutputName = {'Distillate Purity', 'Bottoms Purity'};
DC = setmpcsignals(DC, 'MD', 3);
```

-->Assuming unspecified input signals are manipulated variables.

Review the resulting system.

```
DC
DC =
  From input "Reflux Rate" to output...
                                    12.8
  Distillate Purity: exp(-1*s) * ------
                                 16.7 s + 1
                                 6.6
  Bottoms Purity: exp(-7*s) * ------
                              10.9 s + 1
  From input "Steam Rate" to output...
                                  -18.9
  Distillate Purity: exp(-3*s) * ------
                                 21 s + 1
                                -19.4
   Bottoms Purity: exp(-3*s) * -----
                              14.4 + 1
  From input "Feed Rate" to output...
                                      3.8
   Distillate Purity: exp(-8.1*s) * -----
                                   14.9 s + 1
                                   4.9
   Bottoms Purity: exp(-3.4*s) * -----
                                13.2 s + 1
Input groups:
      Name
                  Channels
    Measured
                    3
   Manipulated
                   1,2
Output groups:
     Name
               Channels
   Measured
                1,2
Continuous-time transfer function.
```

References

[1] Wood, R. K., and M. W. Berry, Chem. Eng. Sci., Vol. 28, pp. 1707, 1973.

See Also

setmpcsignals | ss | tf | zpk

Related Examples

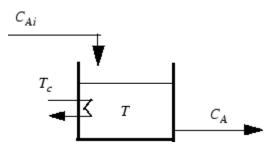
• "Construct Linear Time Invariant (LTI) Models" on page 2-10

CSTR Model

The linearized model of a continuous stirred-tank reactor (CSTR) involving an exothermic (heat-generating) reaction is represented by the following differential equations:

$$\frac{dC'_A}{dt} = a_{11}C'_A + a_{12}T' + b_{11}T'_c + b_{12}C'_{Ai}$$
$$\frac{dT'}{dt} = a_{21}C'_A + a_{22}T' + b_{21}T'_c + b_{22}C'_{Ai}$$

where C_A is the concentration of a key reactant, T is the temperature in the reactor, T_c is the coolant temperature, C_{Ai} is the reactant concentration in the reactor feed, and a_{ij} and b_{ij} are constants. The primes (e.g., C_A) denote a deviation from the nominal steady-state condition at which the model has been linearized.



Measurement of reactant concentrations is often difficult, if not impossible. Let us assume that T is a measured output, C_A is an unmeasured output, T_c is a manipulated variable, and C_{Ai} is an unmeasured disturbance.

The model fits the general state-space format

$$\frac{dx}{dt} = Ax + Bu$$
$$y = Cx + Du$$

where

$$x = \begin{bmatrix} C'_A \\ T' \end{bmatrix}, u = \begin{bmatrix} T'_C \\ C'_{Ai} \end{bmatrix}, y = \begin{bmatrix} T' \\ C'_A \end{bmatrix}$$

$$A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}, B = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix}, C = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}, D = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

The following code shows how to define such a model for some specific values of the a_{ij} and b_{ij} constants:

```
A = [-0.0285 -0.0014

-0.0371 -0.1476];

B = [-0.0850 0.0238

0.0802 0.4462];

C = [0 1

1 0];

D = zeros(2,2);

CSTR = ss(A,B,C,D);
```

The following code sets some of the CSTR model's optional properties:

```
CSTR.InputName = { 'T_c', 'C_A_i'};
CSTR.OutputName = { 'T', 'C_A'};
CSTR.StateName = { 'C_A', 'T'};
CSTR.InputGroup.MV = 1;
CSTR.InputGroup.UD = 2;
CSTR.OutputGroup.MO = 1;
CSTR.OutputGroup.UO = 2;
```

To view the properties of CSTR, enter:

CSTR

Linearize Simulink Models

Generally, real systems are nonlinear. To design an MPC controller for a nonlinear system, you must model the plant in Simulink.

Although an MPC controller can regulate a nonlinear plant, the model used within the controller must be linear. In other words, the controller employs a linear approximation of the nonlinear plant. The accuracy of this approximation significantly affects controller performance.

To obtain such a linear approximation, you *linearize* the nonlinear plant at a specified *operating point*.

Note Simulink Control Design software must be installed to linearize nonlinear Simulink models.

You can linearize a Simulink model:

- From the command line.
- Using the Linear Analysis Tool.
- Using MPC Designer.

Linearization Using MATLAB Code

This example shows how to obtain a linear model of a plant using a MATLAB script.

For this example the CSTR model, CSTR_OpenLoop, is linearized. The model inputs are the coolant temperature (manipulated variable of the MPC controller), limiting reactant concentration in the feed stream, and feed temperature. The model states are the temperature and concentration of the limiting reactant in the product stream. Both states are measured and used for feedback control.

Obtain Steady-State Operating Point

The operating point defines the nominal conditions at which you linearize a model. It is usually a steady-state condition.

Suppose that you plan to operate the CSTR with the output concentration, C_A, at 2 kmol/m^3 . The nominal feed concentration is 10 kmol/m^3 , and the nominal feed

temperature is 300 K. Create an operating point specification object to define the steadystate conditions.

```
opspec = operspec('CSTR OpenLoop');
opspec = addoutputspec(opspec, 'CSTR OpenLoop/CSTR',2);
opspec.Outputs(1).Known = true;
opspec.Outputs(1).y = 2;
op1 = findop('CSTR OpenLoop',opspec);
Operating point search report:
Operating point search report for the Model CSTR_OpenLoop.
 (Time-Varying Components Evaluated at time t=0)
Operating point specifications were successfully met.
States:
(1.) CSTR OpenLoop/CSTR/C A
                                  -4.6e-12 (0)
                   2
    X:
                          dx:
(2.) CSTR OpenLoop/CSTR/T K
          373
                       dx:
                                  5.49e-11 (0)
    X:
Inputs:
(1.) CSTR OpenLoop/Coolant Temperature
          299 [-Inf Inf]
     u:
Outputs:
(1.) CSTR OpenLoop/CSTR
                   2
                        (2)
     V:
```

The calculated operating point is $C_A = 2 \text{ kmol/m}^3$ and $T_K = 373 \text{ K}$. Notice that the steady-state coolant temperature is also given as 299 K, which is the nominal value of the manipulated variable of the MPC controller.

To specify:

- Values of known inputs, use the Input.Known and Input.u fields of opspec
- Initial guesses for state values, use the State.x field of opspec

For example, the following code specifies the coolant temperature as 305 K and initial guess values of the C_A and T_K states before calculating the steady-state operating point:

```
opspec = operspec('CSTR_OpenLoop');
opspec.States(1).x = 1;
opspec.States(2).x = 400;
opspec.Inputs(1).Known = true;
opspec.Inputs(1).u = 305;
op2 = findop('CSTR OpenLoop',opspec);
Operating point search report:
Operating point search report for the Model CSTR OpenLoop.
 (Time-Varying Components Evaluated at time t=0)
Operating point specifications were successfully met.
States:
(1.) CSTR OpenLoop/CSTR/C A
     X:
                1.78
                           dx:
                                  -1.42e-14 (0)
(2.) CSTR_OpenLoop/CSTR/T_K
                  377
                        dx: 5.68e-14 (0)
     X:
Inputs:
(1.) CSTR_OpenLoop/Coolant Temperature
     U:
                  305
Outputs: None
```

Specify Linearization Inputs and Outputs

If the linearization input and output signals are already defined in the model, as in CSTR_OpenLoop, then use the following to obtain the signal set.

io = getlinio('CSTR_OpenLoop');

Otherwise, specify the input and output signals as shown here.

```
io(1) = linio('CSTR_OpenLoop/Coolant Temperature',1,'input');
io(2) = linio('CSTR_OpenLoop/Feed Concentration',1,'input');
```

```
io(3) = linio('CSTR_OpenLoop/Feed Temperature',1,'input');
io(4) = linio('CSTR_OpenLoop/CSTR',1,'output');
io(5) = linio('CSTR_OpenLoop/CSTR',2,'output');
```

Linearize Model

Linearize the model using the specified operating point, op1, and input/output signals, io.

```
sys = linearize('CSTR_OpenLoop',op1,io)
sys =
 A =
          CA TK
         -5 -0.3427
  СА
  ТΚ
         47.68 2.785
 B =
       Coolant Temp Feed Concent Feed Tempera
  СА
                0
                             1
                                           0
               0.3
                              0
                                           1
  ΤК
 C =
          C_A T_K
  CSTR/1
          0
                1
  CSTR/2
          1
                0
 D =
          Coolant Temp Feed Concent Feed Tempera
  CSTR/1
                    0
                                 0
                                              0
                    0
                                 0
                                              0
  CSTR/2
```

Continuous-time state-space model.

Linearization Using Linear Analysis Tool in Simulink Control Design

This example shows how to linearize a Simulink model using the Linear Analysis Tool, provided by the Simulink Control Design product.

This example uses the CSTR model, CSTR_OpenLoop.

Open Simulink Model

sys = 'CSTR_OpenLoop';
open_system(sys)

Open Linear Analysis Tool

In the Simulink model window, select Analysis > Control Design > Linear Analysis.

📣 Linear Analysis	s Tool - CSTR_OpenL	.oop		- 0	×
LINEAR ANALY	/SIS ESTI	MATION PL	OTS AND RESULTS	vew	¢
Load Session Save Session Preferences		Model VOs Model Initial Condition None	Result Viewer Inearization Advisor More Options		
FILE		SETUP	OPTIONS	LINEARIZE	
Data Browser		•			_
Search workspace	variables	₽ +			
MATLAB Works	pace				
Name 🔺	Value				
n sys ▼ Linear Analysis \ Name ▲	'CSTR_Ope Workspace Value				
✓ Variable Preview	v				

Specify Linearization Inputs and Outputs

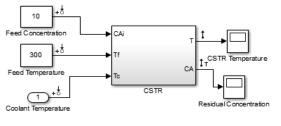
The linearization inputs and outputs are already specified for CSTR_OpenLoop. The input signals correspond to the outputs from the Feed Concentration, Feed Temperature, and Coolant Temperature blocks. The output signals are the inputs to the CSTR Temperature and Residual Concentration blocks.

To specify a signal as a:

- Linearization input, right-click the signal in the Simulink model window and select Linear Analysis Points > Input Perturbation.
- Linearization output, right-click the signal in the Simulink model window and select Linear Analysis Points > Output Measurement.

Specify Residual Concentration as Known Trim Constraint

In the Simulink model window, right-click the CA output signal from the CSTR block. Select Linear Analysis Points > Trim Output Constraint.



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In the Linear Analysis Tool, in the **Linear Analysis** tab, in the **Operating Point** dropdown list, select Trim model.

In the **Outputs** tab:

- Select the Known check box for Channel 1 under CSTR_OpenLoop/CSTR.
- Set the corresponding Value to 2 kmol/m³.

Trim the model					x
Specifications	Options				
States Inputs	Outputs				
				Output Specificat	ions
Output		Value	Known	Minimum	Maximum
CSTR_OpenLoo	op/CSTR				
Channel - 1	(2		-Inf	Inf
		Sync	with Model Impor	t Export	ng Generate MATLAB Script
				-	

Create and Verify Operating Point

In the Trim the model dialog box, click **Start trimming**.

The operating point op_trim1 displays in the Linear Analysis Workspace.

▼ Linear Analysis	Workspace	
Name 🔺	Value	
op_trim1	1x1 Operat	
▼ Variable Previev		
Trimmed operat CSTR_OpenLoop Search finishe point specific	d as: Operating	
successfully m 2 states and 1		

Double click op_trim1 to view the resulting operating point.

In the Edit dialog box, select the **Input** tab.

dit: op_trim1		
Optimizer Output Details		
State Input Output		
Input	Desired Value	Actual Value
CSTR_OpenLoop/Coolant Tempera	ture	
Input - 1	[-Inf , Inf]	299.0349
		Initialize model

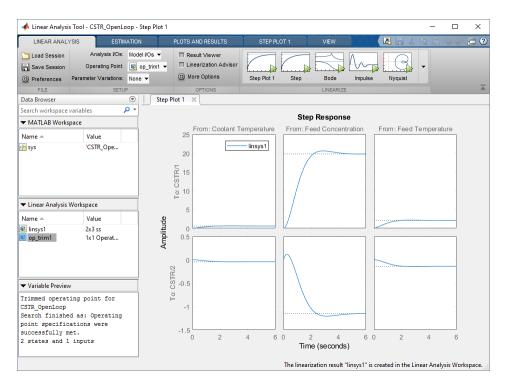
The coolant temperature at steady state is 299 K, as desired.

Linearize Model

In the Linear Analysis tab, in the Operating Point drop-down list, select op_trim1.

Click Step to linearize the model.

This option creates the linear model linsys1 in the Linear Analysis Workspace and generates a step response for this model. linsys1 uses optrim1 as its operating point.



The step response from feed concentration to output CSTR/2 displays an interesting inverse response. An examination of the linear model shows that CSTR/2 is the residual CSTR concentration, C_A. When the feed concentration increases, C_A increases initially because more reactant is entering, which increases the reaction rate. This rate increase results in a higher reactor temperature (output CSTR/1), which further increases the reaction rate and C_A decreases dramatically.

Export Linearization Result

If necessary, you can repeat any of these steps to improve your model performance. Once you are satisfied with your linearization result, in the Linear Analysis Tool, drag and drop it from the **Linear Analysis Workspace** to the **MATLAB Workspace**. You can now use your linear model to design an MPC controller.

See Also

Linear Analysis Tool | linearize

Related Examples

- "Design MPC Controller in Simulink" on page 3-38
- "Design Controller Using MPC Designer" on page 3-2
- "Design MPC Controller at the Command Line" on page 3-24

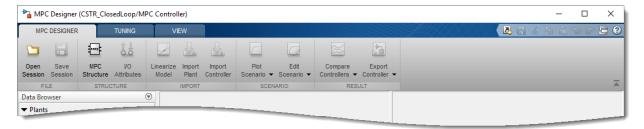
Linearize Simulink Models Using MPC Designer

This topic shows how to linearize Simulink models using **MPC Designer**. To do so, open the app from a Simulink model that contains an MPC Controller block. For this example, use the CSTR_ClosedLoop model.

sys = 'CSTR_ClosedLoop';
open_system(sys)

In the model window, double-click the MPC Controller block.

In the Block Parameters dialog box, ensure that the **MPC Controller** field is empty, and click **Design** to open **MPC Designer**.



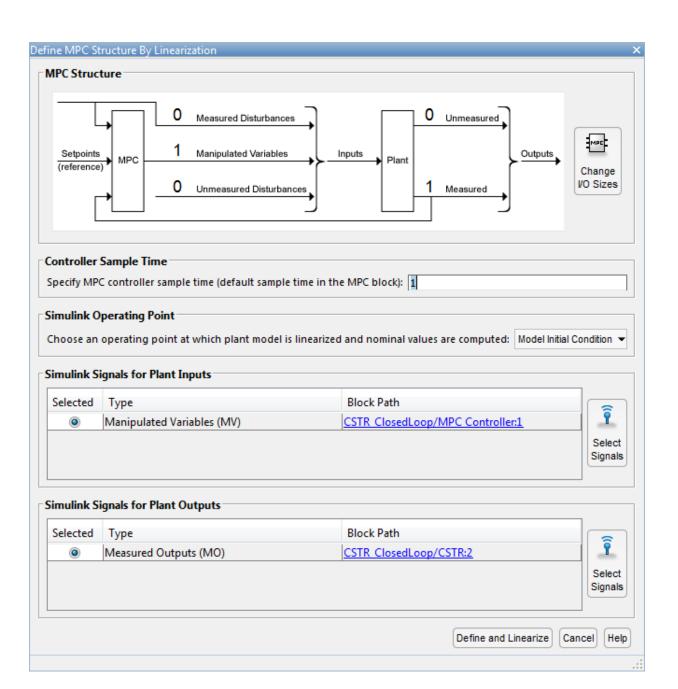
Using **MPC Designer**, you can define the MPC structure by linearizing the Simulink model. After you define the initial MPC structure, you can also linearize the model at different operating points and import the linearized plants.

Note If a controller from the MATLAB workspace is specified in the **MPC Controller** field, the app imports the specified controller. In this case, the MPC structure is derived from the imported controller. In this case, you can still linearize the Simulink model and import the linearized plants.

Define MPC Structure By Linearization

This example shows how to define the plant input/output structure in **MPC Designer** by linearizing a Simulink model.

On the MPC Designer tab, in the Structure section, click MPC Structure.



Specify Signal Dimensions

In the Define MPC Structure By Linearization dialog box, in the **MPC Structure** section, if the displayed signal dimensions do not match your model, click **Change I/O Sizes** to configure the dimensions. Any unmeasured disturbances or unmeasured outputs in your model are not detected by the MPC Controller block. Specify the dimensions for these signals.

MPC Block Signal Sizes	×
Description	
Default signal dimensions used by MPC Controller block are defined in the "Defaul Conditions" tab of the MPC Controller bloc dialog.	
If they are not applicable to your use case, specify correct dimensions below. It will update MPC Controller block before	
Assign plant i/o channels to desired signa	l types:
Number of manipulated variables (MV):	1
Number of measured disturbances (MD):	Not Available
Number of unmeasured disturbances (UD):	1
Number of measured outputs (MO):	1
Number of unmeasured outputs (UO):	0
	OK Cancel Help

Tip In the MPC Controller Block Parameters dialog box, in the **Default Conditions** tab, you can define the controller sample time and signal dimensions before opening **MPC Designer**.

General	Online Features	Default Conditions	Others
Sample T	ime		
MPC contr	roller block sample t	time 1	
Plant Inpu	t Signal Sizes		
Number o	f manipulated varia	bles 1	
Number o	f unmeasured distu	rbances 0	
Plant Outp	out Signal Sizes		
Number o	f measured outputs	1	
Number o	f unmeasured outpu	uts 0	

Select Plant Input/Output Signals

Before linearizing the model, assign Simulink signal lines to each MPC signal type in your model. The app uses these signals as linearization inputs and outputs.

In the **Simulink Signals for Plant Inputs** and **Simulink Signals for Plant Outputs** sections, the **Block Path** is automatically defined for manipulated variables, measured outputs, and measured disturbances. **MPC Designer** detects these signals since they are connected to the MPC Controller block. If your application has unmeasured disturbances or unmeasured outputs, select their corresponding Simulink signal lines.

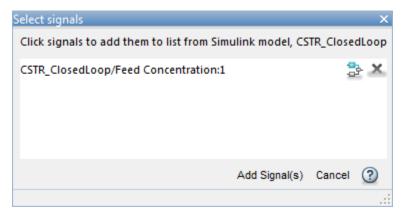
To choose a signal type, use the **Selected** option buttons.

Selected	Туре	Block Path	
	Manipulated Variables (MV)	CSTR ClosedLoop/MPC Controller:1	<u> </u>
۲	Unmeasured Disturbances (UD)	Select a UD signal in the Simulink model	Select
			Signals

Click Select Signals.

In the Simulink model window, click the signal line corresponding to the selected signal type.

The signal is highlighted, and its block path is added to the Select signals dialog box.



In the Select signals dialog box, click Add Signal(s).

In the Define MPC Structure By Linearization dialog box, the **Block Path** for the selected signal type updates.

Note If your model has measured disturbances, you must connect the corresponding plant inputs to the signal line connected to the md port of the MPC Controller block. For more information, see "Connect Measured Disturbances for Linearization" on page 2-50.

Specify Operating Point

In the **Simulink Operating Point** section, in the drop-down list, select an operating point at which to linearize the model.

For information on the different operating point options, see "Specifying Operating Points" on page 2-39.

Note If you select an option that generates multiple operating points for linearization, **MPC Designer** uses only the first operating point to define the plant structure and linearize the model.

Define Structure and Linearize Model

Click **Define and Linearize**.

The app linearizes the Simulink model at the specified operating point using the specified input/output signals, and adds the linearized plant to the **Data Browser**.

Also, a default controller, which uses the linearized plant as its internal model, and a default simulation scenario are created.

MPC Designer uses the input/output signal values at the selected operating point as nominal values.

Linearize Model

After you define the initial MPC structure, you can linearize the Simulink model at different operating points and import the linearized plants. Doing so is useful for validating controller performance against modeling errors.

On the MPC Designer tab, in the Import section, click Linearize Model.

imulink Si	ignals for Plant Inputs		
Selected	Туре	Block Path	
۲	Manipulated Variables (MV)	CSTR ClosedLoop/MPC Controller:1	Î
0			Select
imulink Si	ignals for Plant Outputs		Signals
	ignals for Plant Outputs	Block Path	
imulink S i Selected ©		Block Path CSTR_ClosedLoop/CSTR:2	Signals

Select Plant Input/Output Signals

In the **Simulink Signals for Plant Inputs** and **Simulink Signals for Plant Outputs** sections, the input/output signal configuration is the same as you specified when initially defining the MPC structure.

You cannot change the signal types and dimensions once the structure has been defined. However, for each signal type, you can select different signal lines from your Simulink model. The selected lines must have the same dimensions as defined in the current MPC structure.

Specify Operating Point

In the **Simulink Operating Point** section, in the drop-down list, select the operating points at which to linearize the model.

For information on the different operating point options, see "Specifying Operating Points" on page 2-39.

Linearize Model and Import Plant

Click Linearize and Import.

MPC Designer linearizes the Simulink model at the defined operating point using the specified input/output signals, and adds the linearized plant to the **Data Browser**.

If you select the **Use selected operating point to update nominal values as well** option, the app updates the controller nominal values using the operating point signal values.

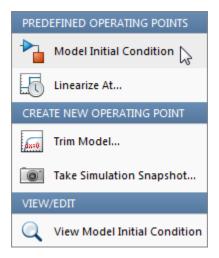
If you select an option that generates multiple operating points for linearization, the app linearizes the model at all the specified operating points. The linearized plants are added to the **Data Browser** in the same order in which their corresponding operating points are defined. If you choose to update the nominal values, the app uses the signal values from the first operating point.

Specifying Operating Points

In the **Simulink Operating Point** section, in the drop-down list, you can select or create operating points for model linearization. For more information on finding steady-state operating points, see "About Operating Points" (Simulink Control Design) and "Compute Steady-State Operating Points from Specifications" (Simulink Control Design).

Select Model Initial Condition

To linearize the model using the initial conditions specified in the Simulink model as the operating point, select **Model Initial Condition**.



The model initial condition is the default operating point for linearization in **MPC Designer**.

Linearize at Simulation Snapshot Times

To linearize the model at specified simulation snapshot times, select **Linearize At**. Linearizing at snapshot times is useful when you know that your model reaches an equilibrium state after a certain simulation time.

PRED	EFINED OPERATING POINTS
	Model Initial Condition
6	Linearize At 🔀
CREA	TE NEW OPERATING POINT
da=0	Trim Model
0	Take Simulation Snapshot
VIEW	/EDIT
Q	View Model Initial Condition

In the Enter snapshot times to linearize dialog box, in the **Simulation snapshot times** field, enter one or more simulation snapshot times. Enter multiple snapshot times as a vector.

Enter snapshot times to linearize	×
Simulation snapshot times (sec):	
[0 5 10]	
	OK Apply Cancel

Click OK.

If you enter multiple snapshot times, and you selected Linearize At from the:

- Define MPC Structure By Linearization dialog box, **MPC Designer** linearizes the model using only the first snapshot time. The nominal values of the MPC controller are defined using the input/output signal values for this snapshot.
- Linearize Simulink Model dialog box, **MPC Designer** linearizes the model at all the specified snapshot times. The linearized plant models are added to the **Data Browser** in the order specified in the snapshot time array. If you selected the **Use selected operating point to update nominal values as well** option, the nominal values are set using the input/output signal values from the first snapshot.

Compute Steady-State Operating Point

To compute a steady-state operating point using numerical optimization methods to meet your specifications, select **Trim Model**.

PRED	EFINED OPERATING POINTS
	Model Initial Condition
6	Linearize At
CREA	TE NEW OPERATING POINT
da=0	Trim Model 🔓
0	Take Simulation Snapshot
VIEW	/EDIT
Q	View Model Initial Condition

In the Trim the model dialog box, enter the specifications for the steady-state values at which you want to find an operating point. You can specify values for states, input signals, and output signals.

Trim the model							×
Specifications	Options						
States Input	s Outputs						
				State Specificat	ions		
State	Value	Known	✓ Steady State	Minimum	Maximum	dx Minimum	dx Maximum
CSTR_ClosedL	oop/CSTR/C_A						
State - 1	10	\checkmark	\checkmark	0	Inf	-Inf	Inf
CSTR_ClosedL	oop/CSTR/T_K						
State - 1	311.267		\checkmark	0	Inf	-Inf	Inf
CSTR_ClosedL	oop/MPC Contro	oller/MPC/last_mv					
State - 1	0			-Inf	Inf	-Inf	Inf
Sync with Model Import Export							
				⊳ s	tart trimming	Generate N	IATLAB Script

Click Start Trimming.

MPC Designer creates an operating point for the given specifications. The computed operating point is added to the **Simulink Operating Point** drop-down list and is selected.

For examples showing how to specify the conditions for a steady-state operating point search, see "Compute Steady-State Operating Points from Specifications" (Simulink Control Design).

Compute Operating Point at Simulation Snapshot Time

To compute operating points using simulation snapshots, select **Take Simulation Snapshot**. Linearizing the model using operating points computed from simulation snapshots is useful when you know that your model reaches an equilibrium state after a certain simulation time.

PRED	EFINED OPERATING POINTS
▶	Model Initial Condition
6	Linearize At
CREA	TE NEW OPERATING POINT
dx=0	Trim Model
0	Take Simulation Snapshot
VIEW	//EDIT
Q	View Model Initial Condition

In the Enter snapshot times to linearize dialog box, in the **Simulation snapshot times** field, enter one or more simulation snapshot times. Enter multiple snapshot times as a vector.

Enter snapshot times to linearize	×
Simulation snapshot times (sec):	
[0 5 10]	
Take Snapshots Generate MATLAB Script Cano	
Take Shapshots Generate MATEAB Script Cano	e

Click Take Snapshots.

MPC Designer simulates the Simulink model. At each snapshot time, the current state of the model is used to create an operating point, which is added to the drop-down list and selected.

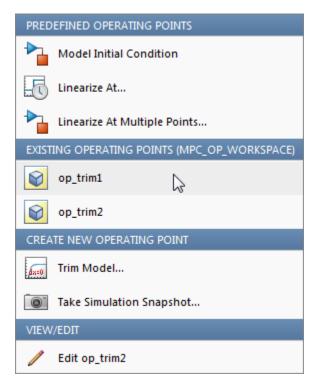
If you entered multiple snapshot times, the operating points are stored together as an array. If you selected **Take Simulation Snapshot** from the:

- Define MPC Structure By Linearization dialog box, **MPC Designer** linearizes the model using only the first operating point in the array. The nominal values of the MPC controller are defined using the input/output signal values for this operating point.
- Linearize Simulink Model dialog box, **MPC Designer** linearizes the model at all the operating points in the array. The linearized plant models are added to the **Data Browser** in the same order as the operating point array.

In **MPC Designer**, the **Linearize At** and **Take Simulation Snapshot** options generally produce the same linearized plant and nominal signal values. However, since the **Take Simulation Snapshot** option first computes an operating point from the snapshot before linearization, the results can differ.

Select Existing Operating Point

Under **Existing Operating Points**, select a previously defined operating point at which to linearize the Simulink model. This option is available if one or more previously created operating points are available in the drop-down list.



If the selected operating point represents an operating point array created using multiple snapshot times, and you selected an operating point from the:

- Define MPC Structure By Linearization dialog box, **MPC Designer** linearizes the model using only the first operating point in the array. The nominal values of the MPC controller are defined using the input/output signal values for this operating point.
- Linearize Simulink Model dialog box, **MPC Designer** linearizes the model at all the operating points in the array. The linearized plant models are added to the **Data Browser** in the same order as the operating point array.

Select Multiple Operating Points

To linearize the Simulink model at multiple existing operating points, select **Linearize at Multiple Points**. This option is available if there are more than one previously created operating points in the drop-down list.

PREDEFINED OPERATING POINTS				
▶	Model Initial Condition			
6	Linearize At			
	Linearize At Multiple Points 📐			
EXISTI	NG OPERATING POINTS (MPC_OP_WORKSPACE)			
	op_snapshot1			
Ŷ	op_trim1			
Ŷ	op_trim2			
CREAT	E NEW OPERATING POINT			
dx=0	Trim Model			
0	Take Simulation Snapshot			
VIEW/	EDIT			
1	Edit op_snapshot1			

ecify mul	tiple operating points	-
Selected	Operating Points	
V	op_trim1	
1	op_trim2	Up
1	op_snapshot1	Dowr
		Edit
		Delete
	OK Cano	el ?

In the Specify multiple operating points dialog box, select the operating points at which to linearize the model.

To change the operating point order, click an operating point in the list and click **Up** or **Down** to move the highlighted operating point within the list.

Click OK.

If you selected Linearize at Multiple Points from the:

- Define MPC Structure By Linearization dialog box, **MPC Designer** linearizes the model using only the first specified operating point. The nominal values of the MPC controller are defined using the input/output signal values for this operating point.
- Linearize Simulink Model dialog box, **MPC Designer** linearizes the model at all the specified operating points. The linearized plant models are added to the **Data Browser** in the order specified in the Specify multiple operating points dialog box.

View/Edit Operating Point

To view or edit the selected operating point, under **View/Edit**, click the **Edit** option.

PREDEFINED OPERATING POINTS							
	Model Initial Condition						
6	Linearize At						
▶	Linearize At Multiple Points						
EXIST	ING OPERATING POINTS (MPC_OP_WORKSPACE)						
	op_snapshot1						
	op_trim1						
	op_trim2						
CREA	TE NEW OPERATING POINT						
da=0	Trim Model						
0	Take Simulation Snapshot						
VIEW	/EDΠ						
1	Edit op_snapshot1 🛛 🍃						

In the Edit dialog box, if you created the selected operating point from a simulation snapshot, you can edit the operating point values.

Edit: op_snapshot3 ×				
Select Operating Point: Operating point originally taken at t = 0				
State	Value			
CSTR_ClosedLoop/CSTR/C_A				
State - 1	8.5695			
CSTR_ClosedLoop/CSTR/T_K				
State - 1	311.267			
CSTR_ClosedLoop/MPC Controller/MPC/last_mv				
State - 1	0			
	Refresh Initialize model			

If the selected operating point represents an operating point array, in the **Select Operating Point** drop-down list, select an operating point to view.

If you obtained the operating point by trimming the model, you can only view the operating point values.

Edit: op_trim1 ×					
Optimizer Output Details					
State Input Output					
State	Desired Value	Actual Value	Desired dx	Actual dx	
CSTR_ClosedLoop/CSTR/C_A					
State - 1	10	10	0	-3.5732e-08	
CSTR_ClosedLoop/CS	STR/T_K				
State - 1	[0, Inf]	161.9721	0	4.3283e-07	
CSTR_ClosedLoop/M	PC Controller/MPC/la	st_mv			
State - 1	[-Inf, Inf]	-298.1209	0	0	
<u> </u>					
				Initialize model	
				.::	

To set the Simulink model initial conditions to the states in the operating point, click **Initialize model**. You can then simulate the model at the specified operating point.

When setting the model initial conditions, **MPC Designer** exports the operating point to the MATLAB workspace. Also, in the Simulink Configuration Parameters dialog box, in the **Data Import/Export** section, it selects the **Input** and **Initial state** parameters and configures them to use the states and inputs in the exported operating point.

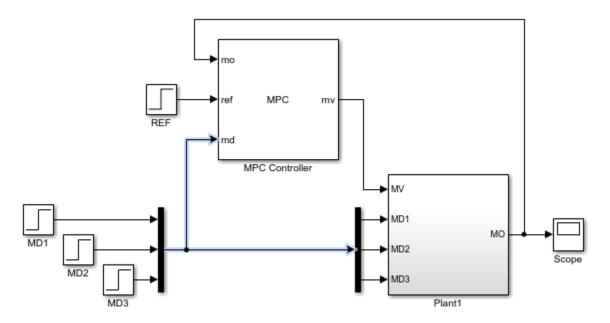
To reset the model initial conditions, for example if you delete the exported operating point, clear the **Input** and **Initial state** parameters.

Connect Measured Disturbances for Linearization

If your Simulink model has measured disturbance signals, connect them to the corresponding plant input ports and to the md port of the MPC Controller block. If you have multiple measured disturbances, connect them to the MPC Controller using a vector signal. As discussed in "Define MPC Structure By Linearization" on page 2-32, **MPC**

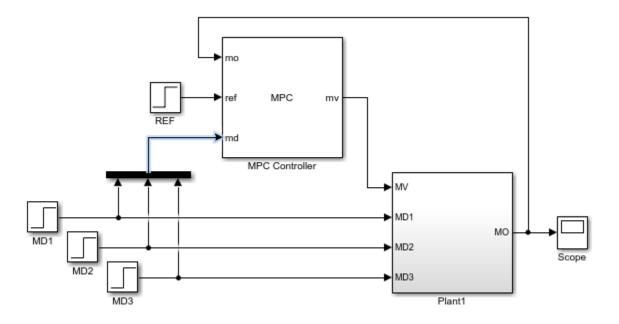
Designer automatically detects the measured disturbances connected to the MPC Controller block and sets them as plant inputs for linearization.

Since the measured disturbances connected to the md port are selected as linearization inputs, you must connect the plant measured disturbance input ports to the selected signal line, as shown in the following:



Correct MD Connection

If you connect the plant measured disturbance input ports to the corresponding signals before the Mux block, as shown in the following, there is no linearization path from the signals at the md port to the plant. As a result, when you linearize the plant using **MPC Designer**, the measured disturbance channels linearize to zero.



Incorrect MD Connection

See Also

MPC Designer

Related Examples

- "Linearize Simulink Models" on page 2-22
- "Design MPC Controller in Simulink" on page 3-38

Identify Plant from Data

When designing a model predictive controller, you can specify the internal predictive plant model using a linear identified model. You use System Identification Toolbox software to estimate a linear plant model in one of these forms:

- State-space model idss
- Transfer function model idtf
- Polynomial model idpoly
- Process model idproc
- Grey-box model idgrey

You can estimate the plant model programmatically at the command line or interactively using the **System Identification** app.

Identify Plant from Data at the Command Line

This example shows how to identify a plant model at the command line. For information on identifying models using the System Identification app, see "Identify Linear Models Using System Identification App" (System Identification Toolbox).

Load the measured input/output data.

load plantIO

This command imports the plant input signal, u, plant output signal, y, and sample time, Ts to the MATLAB® workspace.

Create an iddata object from the input and output data.

```
mydata = iddata(y,u,Ts);
```

You can optionally assign channel names and units for the input and output signals.

```
mydata.InputName = 'Voltage';
mydata.InputUnit = 'V';
mydata.OutputName = 'Position';
mydata.OutputUnit = 'cm';
```

Typically, you must preprocess identification I/O data before estimating a model. For this example, remove the offsets from the input and output signals by detrending the data.

```
mydatad = detrend(mydata);
```

You can also remove offsets by creating an ssestOptions object and specifying the InputOffset and OutputOffset options.

For this example, estimate a second-order, linear state-space model using the detrended data. To estimate a discrete-time model, specify the sample time as Ts.

```
ss1 = ssest(mydatad,2,'Ts',Ts)
ss1 =
  Discrete-time identified state-space model:
    x(t+Ts) = A x(t) + B u(t) + K e(t)
       y(t) = C x(t) + D u(t) + e(t)
  A =
                     x2
            x1
        0.8942 -0.1575
   x1
               0.7616
   х2
        0.1961
  B =
         Voltage
   x1
       6.008e-05
   х2
        -0.01219
  C =
                  x1
                           х2
   Position
               38.24 -0.3835
  D =
             Voltage
   Position
                   0
  K =
       Position
      0.03572
   x1
   х2
         0.0223
Sample time: 0.1 seconds
Parameterization:
   FREE form (all coefficients in A, B, C free).
   Feedthrough: none
   Disturbance component: estimate
   Number of free coefficients: 10
```

```
Use "idssdata", "getpvec", "getcov" for parameters and their uncertainties.
Status:
Estimated using SSEST on time domain data "mydatad".
Fit to estimation data: 89.85% (prediction focus)
FPE: 0.0156, MSE: 0.01541
```

You can use this identified plant as the internal prediction model for your MPC controller. When you do so, the controller converts the identified model to a discrete-time, statespace model.

By default, the MPC controller discards any unmeasured noise components from your identified model. To configure noise channels as unmeasured disturbances, you must first create an augmented state-space model from your identified model. For example:

```
ss2 = ss(ss1, 'augmented')
ss2 =
  A =
           x1
                   x2
   x1
       0.8942 -0.1575
   х2
       0.1961 0.7616
  B =
         Voltage v@Position
       6.008e-05
                    0.004448
   x1
   х2
        -0.01219
                    0.002777
  C =
                 x1
                          х2
   Position
              38.24 -0.3835
  D =
               Voltage v@Position
   Position
                     0
                            0.1245
Input groups:
     Name
               Channels
   Measured
                  1
                   2
    Noise
Sample time: 0.1 seconds
Discrete-time state-space model.
```

This command creates a state-space model, ss2, with two input groups, Measured and Noise, for the measured and noise inputs respectively. When you import the augmented model into your MPC controller, channels in the Noise input group are defined as unmeasured disturbances.

Working with Impulse-Response Models

You can use System Identification Toolbox software to estimate finite step-response or finite impulse-response (FIR) plant models using measured data. Such models, also known as nonparametric models, are easy to determine from plant data ([1] and [2]) and have intuitive appeal.

Use the impulseest function to estimate an FIR model from measured data. This function generates the FIR coefficients encapsulated as an idtf object; that is, a transfer function model with only numerator coefficients. impulseest is especially effective in situations where the input signal used for identification has low excitation levels. To design a model predictive controller for this plant, you can convert the identified FIR plant model to a numeric LTI model. However, this conversion usually yields a high-order plant, which can degrade the controller design. For example, the numerical precision issues with high-order plants can affect estimator design. This result is particularly an issue for MIMO systems.

Model predictive controllers work best with low-order parametric models. Therefore, to design a model predictive controller using measured plant data, you can:

- Estimate a low-order parametric model using a parametric estimator, such as ssest.
- Initially identify a nonparametric model using impulseest, and then estimate a loworder parametric model from the response of the nonparametric model. For an example, see [3].
- Initially identify a nonparametric model using impulseest, and then convert the FIR model to a state-space model using idss. You can then reduce the order of the statespace model using balred. This approach is similar to the method used by ssregest.

References

[1] Cutler, C., and F. Yocum, "Experience with the DMC inverse for identification," *Chemical Process Control* — *CPC IV* (Y. Arkun and W. H. Ray, eds.), CACHE, 1991.

- [2] Ricker, N. L., "The use of bias least-squares estimators for parameters in discrete-time pulse response models," *Ind. Eng. Chem. Res.*, Vol. 27, pp. 343, 1988.
- [3] Wang, L., P. Gawthrop, C. Chessari, T. Podsiadly, and A. Giles, "Indirect approach to continuous time system identification of food extruder," *J. Process Control*, Vol. 14, Number 6, pp. 603–615, 2004.

See Also

Apps System Identification

Functions

detrend|iddata|ssest

More About

- "Handling Offsets and Trends in Data" (System Identification Toolbox)
- "Identify Linear Models Using System Identification App" (System Identification Toolbox)
- "Design MPC Controller for Identified Plant Model"

Design MPC Controllers

- "Design Controller Using MPC Designer" on page 3-2
- "Design MPC Controller at the Command Line" on page 3-24
- "Design MPC Controller in Simulink" on page 3-38
- "Control of a Single-Input-Single-Output Plant" on page 3-59
- "Control of a Multi-Input Single-Output Plant" on page 3-62
- "Control of a Multi-Input Multi-Output Nonlinear Plant" on page 3-96

Design Controller Using MPC Designer

This example shows how to design a model predictive controller for a continuous stirredtank reactor (CSTR) using **MPC Designer**.

CSTR Model

The following differential equations represent the linearized model of a continuous stirred-tank reactor (CSTR) involving an exothermic reaction:

$$\frac{dC'_A}{dt} = a_{11}C'_A + a_{12}T' + b_{11}T'_c + b_{12}C'_{Ai}$$
$$\frac{dT'}{dt} = a_{21}C'_A + a_{22}T' + b_{21}T'_c + b_{22}C'_{Ai}$$

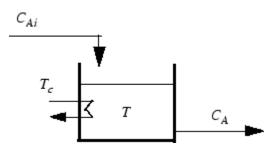
where the inputs are:

- C_{Ai} Concentration of reagent A in the feed stream (kgmol/m³)
- T_c Reactor coolant temperature (degrees C)

and the outputs are:

- *T* Reactor temperature (degrees C)
- C_A Residual concentration of reagent A in the product stream (kgmol/m³)

The prime terms, such as C_A , denote a deviation from the nominal steady-state condition at which the model has been linearized.



Measurement of reagent concentrations is often difficult. For this example, assume that:

• T_c is a manipulated variable.

- C_{Ai} is an unmeasured disturbance.
- *T* is a measured output.
- C_A is an unmeasured output.

The model can be described in state-space format:

$$\frac{dx}{dt} = Ax + Bu$$

$$y = Cx + Du$$

where,

$$x = \begin{bmatrix} C'_{A} \\ T' \end{bmatrix}, u = \begin{bmatrix} T'_{C} \\ C'_{Ai} \end{bmatrix}, y = \begin{bmatrix} T' \\ C'_{A} \end{bmatrix}$$
$$A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}, B = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix}, C = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}, D = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

For this example, the coolant temperature has a limited range of ± 10 degrees from its nominal value and a limited rate of change of ± 4 degrees per sample period.

Create a state-space model of a CSTR system.

A = [-0.0285 -0.0014; -0.0371 -0.1476]; B = [-0.0850 0.0238; 0.0802 0.4462]; C = [0 1; 1 0]; D = zeros(2,2); CSTR = ss(A,B,C,D);

Import Plant and Define MPC Structure

mpcDesigner

📣 MPC Designer							
MPC DESIGNER	TUNING	VIEW				27777 🕐 🛃	
	₩ ĴJ				20		
	IPC VO ucture Attributes STRUCTURE	Import Import Plant Controller	Plot Edit Scenario V Scenario V SCENARIO	Compare Exp Controllers - Control RESULT	oort oller 👻		
Data Browser	SINGOIGHE	Image: Control of the control of	- BOLINARO	I REGOLI			
▼ Plants							
▼ Controllers							
▼ Scenarios							
			To get started, select "	MPC Structure" to imp	port a plant or co	ntroller from MATLAB workspace	nd use it to define I/O channel types.

On the MPC Designer tab, in the Structure section, click MPC Structure.

In the Define MPC Structure By Importing dialog box, in the **Select a plant model or an MPC controller** table, select the CSTR model.

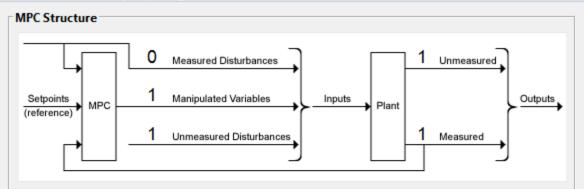
Since CSTR is a stable, continuous-time LTI system, **MPC Designer** sets the controller sample time to 0.1 T_r , where T_r is the average rise time of CSTR. For this example, in the **Specify MPC controller sample time** field, enter a sample time of 1.

By default, all plant inputs are defined as manipulated variables and all plant outputs as measured outputs. In the **Assign plant i/o channels** section, assign the input and output channel indices such that:

• The first input, coolant temperature, is a manipulated variable.

- The second input, feed concentration, is an unmeasured disturbance.
- The first output, reactor temperature, is a measured output.
- The second output, reactant concentration, is an unmeasured output.

Define MPC Structure By Importing



Select a plant model or an MPC controller from MATLAB Workspace:

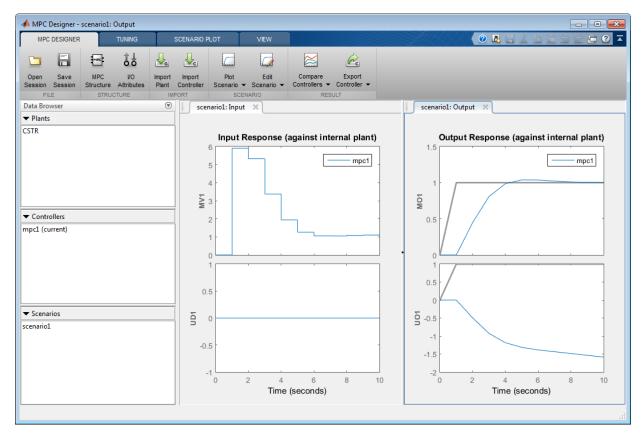
Select	Name	Туре	Order	Inputs	Outputs
۲	CSTR	SS	2	2	2
ntrolle	r Sample Time				
Decity M	PC controller sa	mple time: 1			
sign pla	ant i/o channel	s to desired signal ty	pes:		
lanipula	ted variable (M	V) channel indices:	1		
		1D) channel indices:			
	-				
nmeasu	red disturbance	(UD) channel indices:	2		
leasured	d output (MO) c	hannel indices:	1		
	red output (UO) channel indices:	2		
nmeasu	rea output joo		_		
nmeasu	ica oatpat (oo				
	sh workspace			Define a	nd Import Cancel He

Click Define and Import.

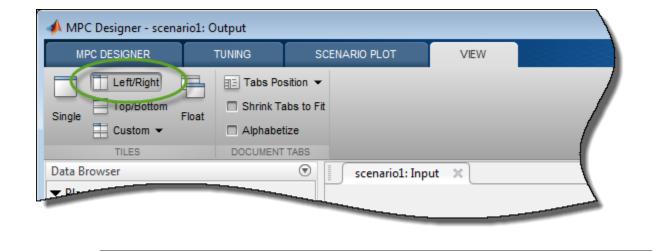
The app imports the CSTR plant to the **Data Browser**. The following are also added to the **Data Browser**:

- mpc1 Default MPC controller created using sys as its internal model.
- scenario1 Default simulation scenario.

The app runs the default simulation scenario and updates the **Input Response** and **Output Response** plots.



Tip To view the response plots side-by-side, on the **View** tab, in the **Tiles** section, click **Left/Right**.



Once you define the MPC structure, you cannot change it within the current **MPC Designer** session. To use a different channel configuration, start a new session of the app.

Define Input and Output Channel Attributes

On the MPC Designer tab, select I/O Attributes.

In the Input and Output Channel Specifications dialog box, in the **Name** column, specify a meaningful name for each input and output channel.

In the **Unit** column, optionally specify the units for each channel.

Since the state-space model is defined using deviations from the nominal operating point, set the **Nominal Value** for each input and output channel to 0.

Keep the **Scale Factor** for each channel at the default value of 1.

u(1) u(2)	MV UD	Tc CAi	deg C kgmol/m^3	0	1
u(2)	UD	CAi	kamol/m^3	0	
			kgm0i/m*5	0	1
M3	Туре	-	1	0	la
y(1)	MO	T	deg C	0	1
y(2)	UO	CA	kgmol/m^3	0	1

Click OK.

The **Input Response** and **Output Response** plot labels update to reflect the new signal names and units.

Configure Simulation Scenario

On the **MPC Designer** tab, in the **Scenario** Section, click **Edit Scenario** > **scenario1**.

In the Simulation Scenario dialog box, increase the **Simulation duration** to 30 seconds.

In the **Reference Signals** table, in the first row, specify a step **Size** of 2 and a **Time** of 5.

In the **Signal** column, in the second row, select a **Constant** reference to hold the concentration setpoint at its nominal value.

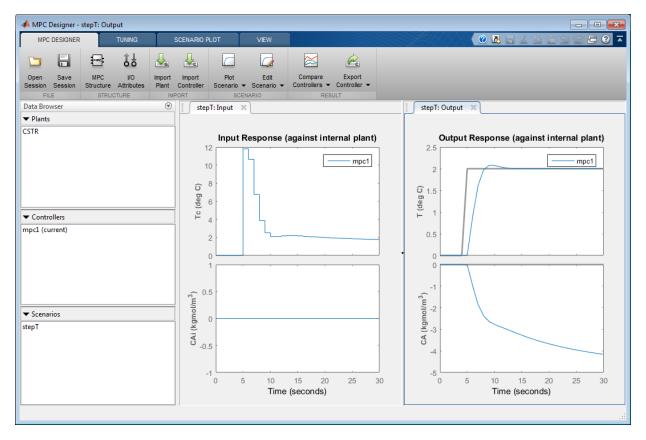
Plant	t used in simul	lation: Defau	It (controller in	ternal mode	an a	-
			ne (controller in	ternar mout	.17	-
Simulation	n duration (see	conds) 30				
-		- 1°				
Run o	pen-loop simula	ation	Use unconst	rained MPC		
🔲 Previe	w references	(look ahead)	Preview mea	sured distu	bances (look al	head)
Previe	w references	(look ahead)	Preview mea	asured distu	bances (look al	head)
				asured distu	bances (look al	head)
		(look ahead) oints for all o		asured distu	bances (look al	head)
eference				sured distur	bances (look al	head) Period
	Signals (setpo	oints for all o	utputs) Signal			

The default scenario is configured to simulate a step change of 2 degrees in the reactor temperature, T, at a time of 5 seconds.

Click OK.

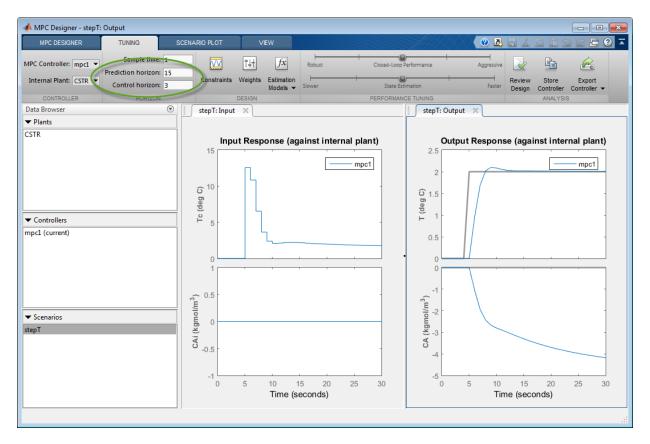
The response plots update to reflect the new simulation scenario configuration.

In the **Data Browser**, in the **Scenarios** section, double-click scenario1, and rename the scenario as stepT.



Configure Controller Horizons

On the Tuning tab, in the Horizons section, specify a $Prediction\ horizon\ of\ 15\ and\ a\ Control\ horizon\ of\ 3.$



The response plots update to reflect the new horizons. The **Input Response** plot shows that the control actions for the manipulated variable violate the required coolant temperature constraints.

Define Input Constraints

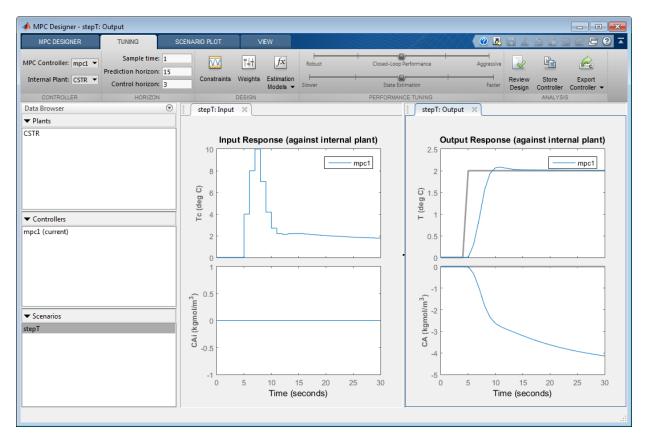
In the **Design** section, click **Constraints**.

In the Constraints dialog box, in the **Input Constraints** section, enter the coolant temperature upper and lower bounds in the **Min** and **Max** columns respectively.

Specify the rate of change limits in the **RateMin** and **RateMax** columns.

Channel	Туре	Min	Max	RateMin	RateMax
(1)	MV	-10	10	-4	4

Click OK.



The **Input Response** plot shows the constrained manipulated variable control actions. Even with the constrained rate of change, the coolant temperature rises quickly to its maximum limit within three control intervals.

Specify Controller Tuning Weights

On the **Tuning** tab, in the **Design** section, click **Weights**.

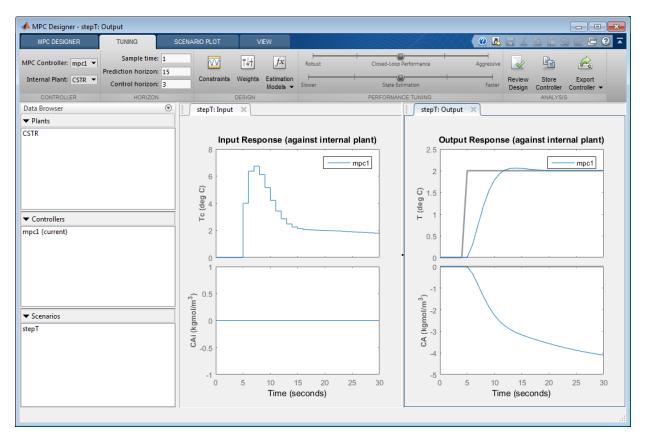
In the **Input Weights** table, increase the manipulated variable (MV) **Rate Weight** to 0.3. Increasing the MV rate weight penalizes large MV changes in the controller optimization cost function.

In the **Output Weights** table, keep the default **Weight** values. By default, all unmeasured outputs have zero weights.

Since there is only one manipulated variable, if the controller tries to hold both outputs at specific setpoints, one or both outputs will exhibit steady-state error in their responses. Since the controller ignores setpoints for outputs with zero weight, setting the concentration output weight to zero allows reactor temperature setpoint tracking with zero steady-state error.

Channel	Туре	Weight	Rate Weight	Target
J(1)	MV	0	0.3	nominal
utput Wei	ights (dime	nsionless)		
· ·	-			
Channel		Туре	Weight	
		Type MO	Weight 1	
/(1)				
/(1)		MO	1	
/(1)		MO	1	
/(1)		MO	1	
γ(1) γ(2)	· · · · ·	MO UO	1	
/(1) /(2)	t (dimension	MO UO	1	
y(1) y(2) CR Weight		MO UO nless)	1	
y(1) y(2) CR Weight		MO UO	1	
y(1) y(2) CR Weight		MO UO nless)	1	ply] Cancel [

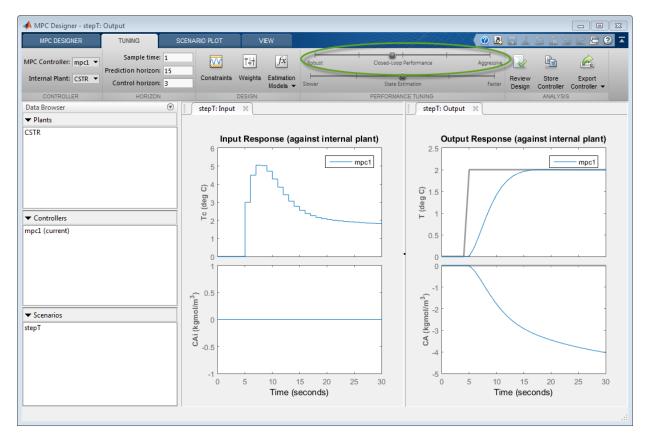
Click OK.



The **Input Response** plot shows the more conservative control actions, which result in a slower **Output Response**.

Eliminate Output Overshoot

Suppose the application demands zero overshoot in the output response. On the **Performance Tuning** tab, drag the **Closed-Loop Performance** slider to the left until the **Output Response** has no overshoot. Moving this slider to the left simultaneously increases the manipulated variable rate weight of the controller and decreases the output variable weight, producing a more robust controller.



When you adjust the controller tuning weights using the **Closed-Loop Performance** slider, **MPC Designer** does not change the weights you specified in the Weights dialog box. Instead, the slider controls an adjustment factor, which is used with the user-specified weights to define the actual controller weights.

This factor is 1 when the slider is centered; its value decreases as the slider moves left and increases as the slider moves right. The weighting factor multiplies the manipulated variable and output variable weights and divides the manipulated variable rate weights from the Weights dialog box.

To view the actual controller weights, export the controller to the MATLAB workspace, and view the Weights property of the exported controller object.

Test Controller Disturbance Rejection

In a process control application, disturbance rejection is often more important than setpoint tracking. Simulate the controller response to a step change in the feed concentration unmeasured disturbance.

On the **MPC Designer** tab, in the **Scenario** section, click **Plot Scenario** > **New Scenario**.

In the Simulation Scenario dialog box, set the **Simulation duration** to 30 seconds.

In the Unmeasured Disturbances table, in the Signal drop-down list, select Step.

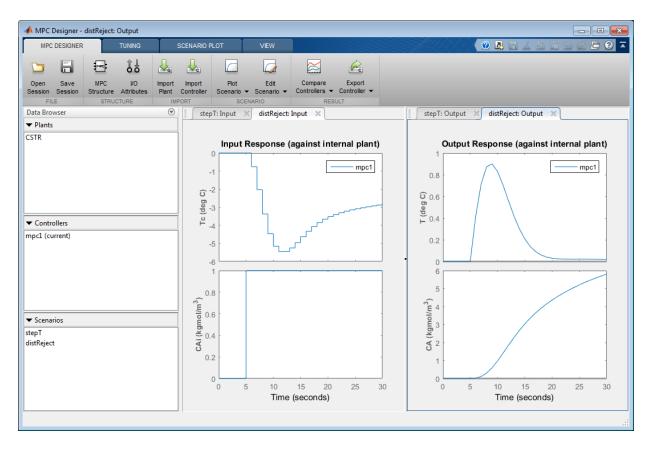
In the **Time** column, specify a step time of 5 seconds.

imulation	Settings					
Plant	used in simu	lation: Defau	lt (controller in	ternal mode	el)	
Simulation	duration (se	conds) 30				
	pen-loop simula w references		Use unconst Preview mea		bances (look al	head)
eference	Signals (setp	oints for all o	utputs)			
Channel	Signals (setpo Name	Nominal	u tputs) Signal	Size	Time	Period
					Time	Period
Channel	Name	Nominal	Signal		Time	Period
Channel (1) (2)	Name Ref of T Ref of CA	Nominal 0 0	Signal		Time	Period

Click OK.

The app adds new scenario to the **Data Browser** and creates new corresponding **Input Response** and **Output Response** plots.

In the **Data Browser**, in the **Scenarios** section, double-click NewScenario, and rename it distReject.



In the **Output Response** plots, the controller returns the reactor temperature, \mathbf{T} , to a value near its setpoint as expected. However, the required control actions cause an increase in the output concentration, **CA** to 6 kgmol/m³.

Specify Concentration Output Constraint

Previously, you defined the controller tuning weights to achieve the primary control objective of tracking the reactor temperature setpoint with zero steady-state error. Doing so enables the unmeasured reactor concentration to vary freely. Suppose that unwanted reactions occur once the reactor concentration exceeds a 3 kgmol/m³. To limit the reactor concentration, specify an output constraint.

On the **Tuning** tab, in the **Design** section, click **Constraints**.

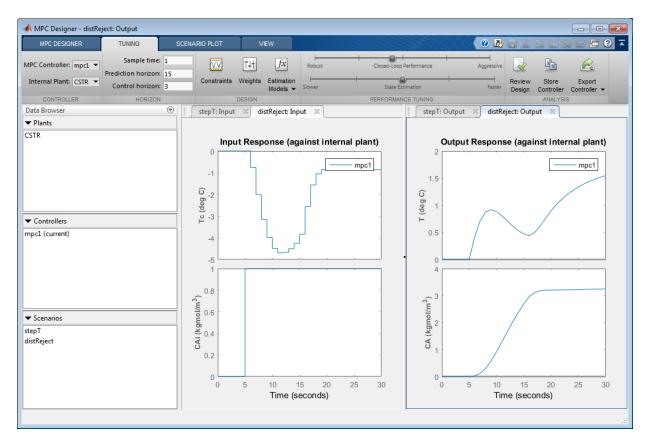
In the Constraints dialog box, in the **Output Constraints** section, the second row of the table, specify a **Max** unmeasured output (UO) value of **3**.

In the **Output Constraints** section, click **Constraint Softening Settings**.

By default, all output constraints are soft, meaning that their **MinECR** and **MaxECR** values are greater than zero. To soften the unmeasured output (UO) constraint further, increase its **MaxECR** value.

Channel	Туре	Min	Max
y(1)	MO	-Inf	Inf
y(2)	UO	-Inf	3
- Constraint Soft Channel		MinECR	MaxECR
Channel	Туре	MinECR	MaxECR
Channel y(1)	Type MO	MinECR 1	1
- Constraint Soft Channel y(1) y(2)	Туре	MinECR 1 1	

Click OK.



In the **Output Response** plots, once the reactor concentration, **CA**, approaches 3 kgmol/m³, the reactor temperature, **T**, starts to increase. Since there is only one manipulated variable, the controller makes a compromise between the two competing control objectives: Temperature control and constraint satisfaction. A softer output constraint enables the controller to sacrifice the constraint requirement more to achieve improved temperature tracking.

Since the output constraint is soft, the controller maintain adequate temperature control by allowing a small concentration constraint violation. In general, depending on your application requirements, you can experiment with different constraint settings to achieve an acceptable control objective compromise.

Export Controller

In the **Tuning** tab, in the **Analysis** section, click **Export Controller** is to save the tuned controller, mpc1, to the MATLAB workspace.

Delete Plants, Controllers, and Scenarios

To delete a plant, controller, or scenario, in the **Data Browser**, right-click the item you want to delete, and select **Delete**. You can also click the item and hit **Delete** on the keyboard.

You cannot delete the current controller. Also, you cannot delete a plant or scenario if it is the only listed plant or scenario.

If a plant is used by any controller or scenario, you cannot delete the plant.

To delete multiple plants, controllers, or scenarios, hold **Shift** and click each item that you want to delete.

References

[1] Seborg, D. E., T. F. Edgar, and D. A. Mellichamp, Process Dynamics and Control, 2nd Edition, Wiley, 2004, pp. 34-36 and 94-95.

See Also

MPC Designer

More About

- "Specify Constraints"
- "Tune Weights"
- "Design MPC Controller in Simulink" on page 3-38

Design MPC Controller at the Command Line

This example shows how to create and test a model predictive controller from the command line.

Define Plant Model

This example uses the plant model described in "Design Controller Using MPC Designer" on page 3-2. Create a state space model of the plant and set some of the optional model properties.

```
A = [-0.0285 -0.0014; -0.0371 -0.1476];
B = [-0.0850 0.0238; 0.0802 0.4462];
C = [0 1; 1 0];
D = zeros(2,2);
CSTR = ss(A,B,C,D);
CSTR.InputName = {'T_c','C_A_i'};
CSTR.OutputName = {'T','C_A'};
CSTR.StateName = {'C_A','T'};
CSTR.InputGroup.MV = 1;
CSTR.InputGroup.UD = 2;
```

Create Controller

CSTR.OutputGroup.M0 = 1; CSTR.OutputGroup.U0 = 2;

To improve the clarity of the example, suppress Command Window messages from the MPC controller.

```
old_status = mpcverbosity('off');
```

Create a model predictive controller with a control interval, or sample time, of 1 second, and with all other properties at their default values.

```
Ts = 1;
MPCobj = mpc(CSTR,Ts);
```

Display the controller properties in the Command Window.

```
display(MPCobj)
```

MPC object (created on 02-Mar-2019 13:36:52):

```
Sampling time: 1 (seconds)
Prediction Horizon: 10
Control Horizon: 2
Plant Model:
     1 manipulated variable(s) -->| 2 states
                                                 |--> 1 measured output(s)
     0 measured disturbance(s) -->| 2 inputs
                                                  |--> 1 unmeasured output(s)
     1 unmeasured disturbance(s) -->| 2 outputs
Indices:
                 Manipulated variables: [1 ]
  (input vector)
                 Unmeasured disturbances: [2]
                       Measured outputs: [1]
  (output vector)
                      Unmeasured outputs: [2]
Disturbance and Noise Models:
       Output disturbance model: default (type "getoutdist(MPCobj)" for details)
        Input disturbance model: default (type "getindist(MPCobj)" for details)
        Measurement noise model: default (unity gain after scaling)
Weights:
       ManipulatedVariables: 0
   ManipulatedVariablesRate: 0.1000
            OutputVariables: [1 0]
                        ECR: 100000
State Estimation: Default Kalman Filter (type "getEstimator(MPCobj)" for details)
Unconstrained
```

View and Modify Controller Properties

Display a list of the controller properties and their current values.

get(MPCobj)

```
Ts: 1

PredictionHorizon (P): 10

ControlHorizon (C): 2

Model: [1x1 struct]

ManipulatedVariables (MV): [1x1 struct]
```

```
OutputVariables (OV): [1x2 struct]
DisturbanceVariables (DV): [1x1 struct]
Weights (W): [1x1 struct]
Optimizer: [1x1 struct]
Notes: {}
UserData: []
History: 02-Mar-2020 13:36:52
```

The displayed History value will be different for your controller, since it depends on when the controller was created. For a description of the editable properties of an MPC controller, enter mpcprops at the command line.

Use dot notation to modify these properties. For example, change the prediction horizon to 15.

MPCobj.PredictionHorizon = 15;

You can abbreviate property names provided that the abbreviation is unambiguous.

Many of the controller properties are structures containing additional fields. Use dot notation to view and modify these field values. For example, you can set the measurement units for the controller output variables. The OutputUnit property is for display purposes only and is optional.

```
MPCobj.Model.Plant.OutputUnit = {'Deg C', 'kmol/m^3'};
```

By default, the controller has no constraints on manipulated variables and output variables. You can view and modify these constraints using dot notation. For example, set constraints for the controller manipulated variable.

```
MPCobj.MV.Min = -10;
MPCobj.MV.Max = 10;
MPCobj.MV.RateMin = -3;
MPCobj.MV.RateMax = 3;
```

You can also view and modify the controller tuning weights. For example, modify the weights for the manipulated variable rate and the output variables.

```
MPCobj.W.ManipulatedVariablesRate = 0.3;
MPCobj.W.OutputVariables = [1 0];
```

You can also define time-varying constraints and weights over the prediction horizon, which shifts at each time step. Time-varying constraints have a nonlinear effect when they

are active. For example, to force the manipulated variable to change more slowly towards the end of the prediction horizon, enter:

MPCobj.MV.RateMin = [-4; -3.5; -3; -2.5];

MPCobj.MV.RateMax = [4; 3.5; 3; 2.5];

The -2.5 and 2.5 values are used for the fourth step and beyond.

Similarly, you can specify different output variable weights for each step of the prediction horizon. For example, enter:

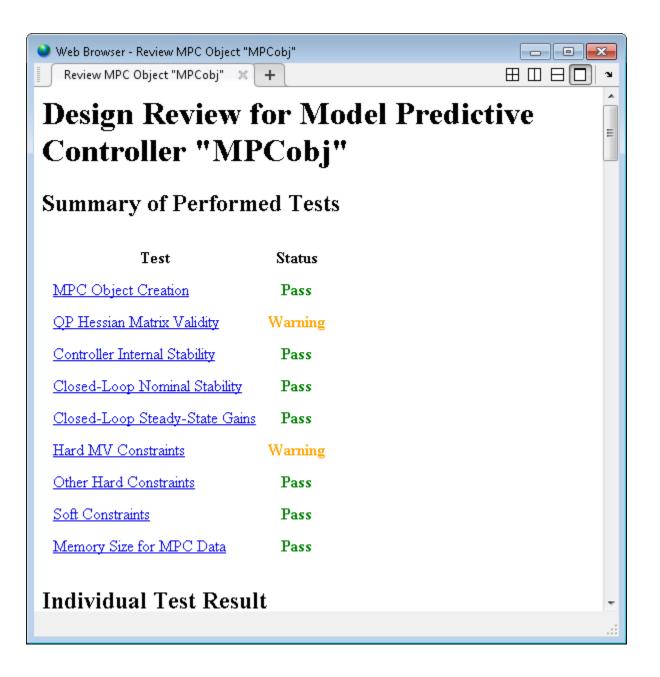
MPCobj.W.OutputVariables = [0.1 0; 0.2 0; 0.5 0; 1 0];

You can also modify the disturbance rejection characteristics of the controller. See setEstimator, setindist and setoutdist for more information.

Review Controller Design

Generate a report on potential run-time stability and performance issues.

review(MPCobj)

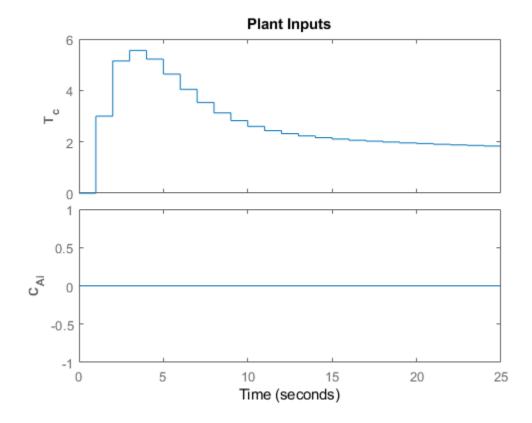


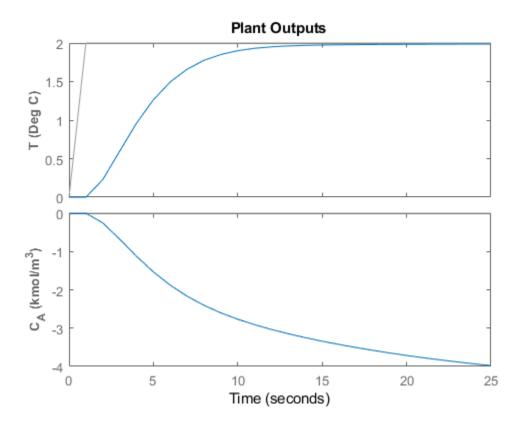
In this example, the <code>review</code> command found two potential issues with the design. The first warning asks whether the user intends to have a weight of zero on the C_A output. The second warning advises the user to avoid having hard constraints on both MV and MVRate.

Perform Linear Simulations

Use the sim function to run a linear simulation of the system. For example, simulate the closed-loop response of MPCobj for 26 control intervals. Specify setpoints of 2 and 0 for the reactor temperature and the residual concentration respectively. The setpoint for the residual concentration is ignored because the tuning weight for the second output is zero.

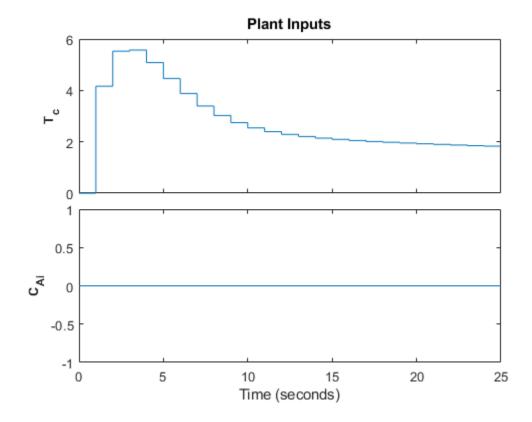
T = 26; r = [0 0; 2 0]; sim(MPCobj,T,r)

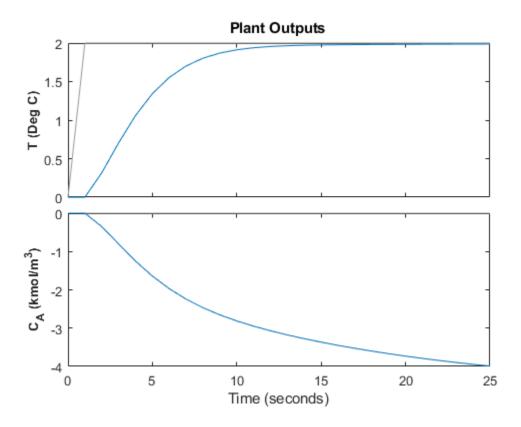




You can modify the simulation options using mpcsimopt. For example, run a simulation with the manipulated variable constraints turned off.

MPCopts = mpcsimopt; MPCopts.Constraints = 'off'; sim(MPCobj,T,r,MPCopts)

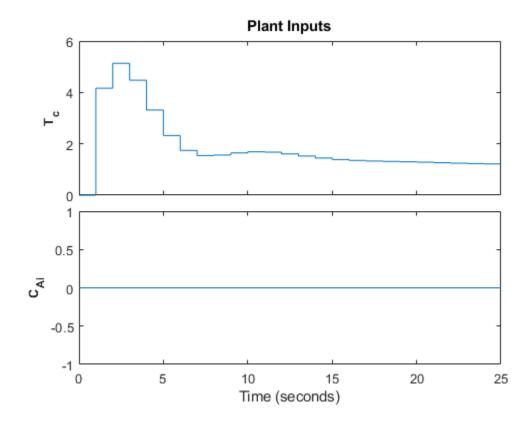


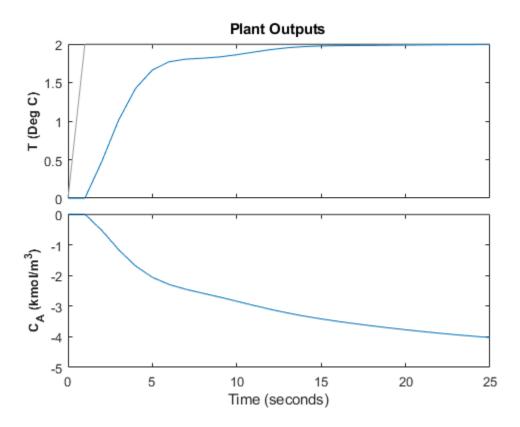


The first move of the manipulated variable now exceeds the specified 3-unit rate constraint.

You can also perform a simulation with a plant/model mismatch. For example, define a plant with 50% larger gains than those in the model used by the controller.

Plant = 1.5*CSTR; MPCopts.Model = Plant; sim(MPCobj,T,r,MPCopts)





The plant/model mismatch degrades controller performance slightly. Degradation can be severe and must be tested on a case-by-case basis.

Other options include the addition of a specified noise sequence to the manipulated variables or measured outputs, open-loop simulations, and a look-ahead option for better setpoint tracking or measured disturbance rejection.

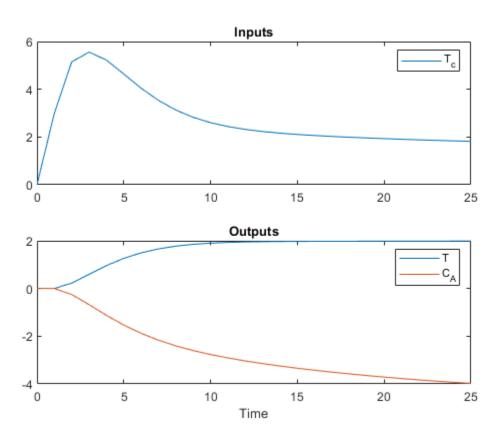
Store Simulation Results

Store the simulation results in the MATLAB Workspace.

[y,t,u] = sim(MPCobj,T,r);

The syntax suppresses automatic plotting and returns the simulation results. You can use the results for other tasks, including custom plotting. For example, plot the manipulated variable and both output variables in the same figure.

```
figure
subplot(2,1,1)
plot(t,u)
title('Inputs')
legend('T_c')
subplot(2,1,2)
plot(t,y)
title('Outputs')
legend('T','C_A')
xlabel('Time')
```



Restore the mpcverbosity setting.

mpcverbosity(old_status);

See Also

mpc|review|sim

More About

- "MPC Modeling" on page 2-2
- "Design Controller Using MPC Designer" on page 3-2
- "Design MPC Controller in Simulink" on page 3-38

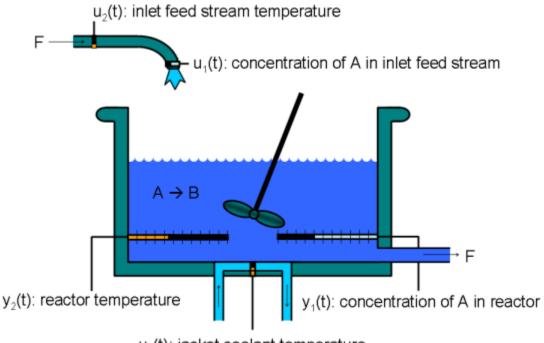
Design MPC Controller in Simulink

This example shows how to design a model predictive controller for a continuous stirredtank reactor (CSTR) in Simulink using **MPC Designer**.

This example requires Simulink Control Design software to define the MPC structure by linearizing a nonlinear Simulink model.

CSTR Model

A CSTR is a jacketed nonadiabatic tank reactor commonly used in the process industry.



u₃(t): jacket coolant temperature

An inlet stream of reagent *A* feeds into the tank at a constant rate. A first-order, irreversible, exothermic reaction takes place to produce the product stream, which exits the reactor at the same rate as the input stream.

The CSTR model has three inputs:

- Feed Concentration (CAi) The concentration of reagent A in the feed stream (kgmol/m³)
- Feed Temperature (*Ti*) Feed stream temperature (K)
- Coolant Temperature (*Tc*) Reactor coolant temperature (K)

The two model outputs are:

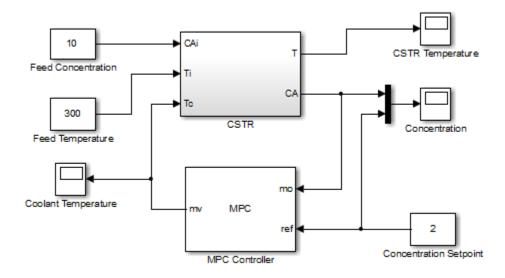
- CSTR Temperature (T) Reactor temperature (K)
- Concentration (*CA*) Concentration of reagent *A* in the product stream, also referred to as the residual concentration (kgmol/m³)

The control objective is to maintain the residual concentration, *CA*, at its nominal setpoint by adjusting the coolant temperature, *Tc*. Changes in the feed concentration, *CAi*, and feed temperature, *Ti*, cause disturbances in the CSTR reaction.

The reactor temperature, *T*, is usually controlled. However, for this example, ignore the reactor temperature, and assume that the residual concentration is measured directly.

Open Simulink Model

open_system('CSTR_ClosedLoop');



Connect Measured Disturbance To MPC Controller Block

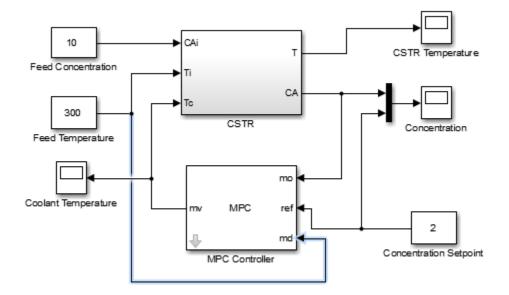
In the Simulink model window, double-click the MPC Controller block.

In the Block Parameters dialog box, on the **General** tab, in the **Additional Inports** section, check the **Measured disturbance (md)** option.

Block Optior	IS			
General	Online Features	Default Conditions	Others	
Additiona	Inports			
Measu	red disturbance (mo	d)		
Extern	al manipulated varia	able (ext.mv)		
Additiona	Outnorts			

Click **Apply** to add the md inport to the controller block.

In the Simulink model window, connect the Feed Temperature block output to the md inport.



Open MPC Designer App

In the MPC Controller Block Parameters dialog box, click **Design** to open **MPC Designer**.

Define MPC Structure

In MPC Designer, on the MPC Designer tab, in the Structure section, click MPC Structure.

In the Define MPC Structure By Linearization dialog box, in the **Controller Sample Time** section, specify a sample time of 0.1.

In the **MPC Structure** section, click **Change I/O Sizes** to add the unmeasured disturbance and measured disturbance signal dimensions.

In the MPC Block Signal Sizes dialog box, specify the number of input/output channels of each type:

IPC Block Signal Sizes	×
Description	
Default signal dimensions used by MPC Controller block are defined in the "Defaul Conditions" tab of the MPC Controller block	•
dialog.	MD Plant
If they are not applicable to your use case, specify correct dimensions below. It will update MPC Controller block before	
Assign plant i/o channels to desired signa	I types:
Number of manipulated variables (MV):	1
Number of measured disturbances (MD):	1
Number of unmeasured disturbances (UD):	1
Number of measured outputs (MO):	1
Number of unmeasured outputs (UO):	0
	OK Cancel Help

Click OK.

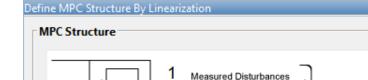
In the Define MPC Structure By Linearization dialog box, in the **Simulink Signals for Plant Inputs** section, the app adds a row for **Unmeasured Disturbances (UD)**.

Outputs

MPC

Change

VO Sizes



1

1

Controller Sample Time

Setpoints

(reference)

Specify MPC controller sample time (default sample time in the MPC block): 0.1

Manipulated Variables

Unmeasured Disturbances

Simulink Operating Point

Choose an operating point at which plant model is linearized and nominal values are computed: Model Initial Condition 💌

Inputs

0

1

Plant

Unmeasured

Measured

Simulink Signals for Plant Inputs

MPC

Selected	Туре	Block Path	
۲	Manipulated Variables (MV)	CSTR ClosedLoop/MPC Controller:1	
0	Measured Disturbances (MD)	CSTR ClosedLoop/Feed Temperature:1	Select
0	Unmeasured Disturbances (UD)	Select a UD signal in the Simulink model	Signals

Simulink Signals for Plant Outputs Selected Type Block Path Measured Outputs (MO) CSTR ClosedLoop/CSTR:2 Select Signals Select Define and Linearize Cancel

The manipulated variable, measured disturbance, and measured output are already assigned to their respective Simulink signal lines, which are connected to the MPC Controller block.

In the **Simulink Signals for Plant Inputs** section, select the **Unmeasured Disturbances (UD)** row, and click **Select Signals**.

In the Simulink model window, click the output signal from the Feed Concentration block.

The signal is highlighted and its block path is added to the Select Signal dialog box.

Select signals	×
Click signals to add them to list from Simulink model, C	TR_ClosedLoop
CSTR_ClosedLoop/Feed Concentration:1	≫ ×
Add Signal(s)	Cancel 🥐

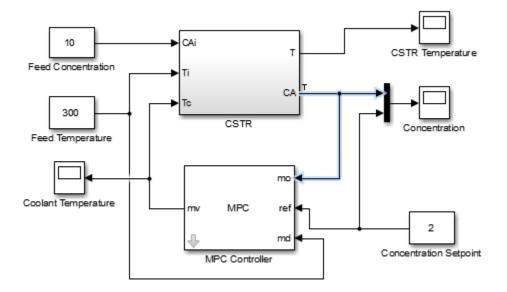
In the Select Signals dialog box, click Add Signal(s).

In the Define MPC Structure By Linearization dialog box, in the **Simulink Signals for Plant Inputs** table, the **Block Path** for the unmeasured disturbance signal is updated.

Linearize Simulink Model

Linearize the Simulink model at a steady-state equilibrium operating point where the residual concentration is 2 kgmol/m^3 . To compute such an operating point, add the CA signal as a trim output constraint, and specify its target constraint value.

In the Simulink model window, right-click the signal line connected to CA outport of the CSTR block, and click Linear Analysis Points > Trim Output Constraint.



The CA signal can now be used to define output specifications for calculating a model steady-state operating point.

In the Define MPC Structure By Linearization dialog box, in the **Simulink Operating Point** section, in the drop-down list, under **Create New Operating Point**, click **Trim Model**.

In the Trim the model dialog box, in the **Outputs** tab, check the box in the **Known** column for Channel-1 and specify a **Value** of 2.

Trim the model				×
Specifications Opt	ions			
States Inputs Out	tputs			
Outrust	Value		Output Specific	ations
Output	Value	Known	Minimum	Maximum
CSTR_ClosedLoop/	SIR			
Channel - 1 🧹	2	V	-Inf	Inf
	Sync wi	th Model Imp	ort	
	Jine wi		Start trimming	Generate MATLAB Script
			ig	

This setting constrains the value of the output signal during the operating point search to a known value.

Click Start Trimming.

In the Define MPC Structure By Linearization dialog box, in the **Simulink Operating Point** section, the computed operating point, op_trim1, is added to the drop-down list and selected.

In the drop-down list, under View/Edit, click Edit op_trim1.

Edit: op_trim1 ×						
Optimizer Output D	etails					
State Input Outpu	t					
State	Desired Value	Actual Value	Desired dx	Actual dx		
CSTR_ClosedLoop/CS	STR/C_A					
State - 1	[0, Inf]	2	0	-4.5972e-12		
CSTR_ClosedLoop/CSTR/T_K						
State - 1	[0, Inf]	373.1311	0	5.4897e-11		
CSTR_ClosedLoop/M	PC Controller/MPC/la	st_mv				
State - 1	[-Inf, Inf]	299.0349	0	0		
<u></u>				Initialize model		
				.::		

In the Edit dialog box, on the **State** tab, in the **Actual dx** column, the near-zero derivative values indicate that the computed operating point is at steady-state.

Click **Initialize model** to set the initial states of the Simulink model to the operating point values in the **Actual Values** column. Doing so enables you to later simulate the Simulink model at the computed operating point rather than at the default model initial conditions.

In the Initialize Model dialog box, click **OK**.

When setting the model initial conditions, **MPC Designer** exports the operating point to the MATLAB workspace. Also, in the Simulink Configuration Parameters dialog box, in the **Data Import/Export** section, it selects the **Input** and **Initial state** parameters and configures them to use the states and inputs in the exported operating point.

To reset the model initial conditions, for example if you delete the exported operating point, clear the **Input** and **Initial state** parameters.

Close the Edit dialog box.

In the Define MPC Structure By Linearization dialog box, click **Define and Linearize** to linearize the model.

The linearized plant model is added to the **Data Browser**. Also, the following are added to the **Data Browser**:

- A default MPC controller created using the linearized plant as an internal prediction model
- A default simulation scenario

Define Input/Output Channel Attributes

On the MPC Designer tab, in the Structure section, click I/O Attributes.

In the Input and Output Channel Specifications dialog box, in the **Name** column, specify meaningful names for each input and output channel.

In the **Unit** column, specify appropriate units for each signal.

Channel	Туре	Name	Unit	Nominal Value	Scale Factor
u(1)	MV	Tc	deg K	299.034880275325	1
u(2)	MD	Ti	deg K	300	1
u(3)	UD	CAi	kgmol/m^3	0	1
Plant Outpu		Name	Unit	Nominal Value	Scale Factor
'lant Outpu Channel	ts Type	Name	Unit	Nominal Value	Scale Factor
-		Name CA	Unit kgmol/m^3		Scale Factor

The **Nominal Value** for each signal is the corresponding steady-state value at the computed operating point.

Click OK.

Define Disturbance Rejection Simulation Scenarios

The primary objective of the controller is to hold the residual concentration, CA, at the nominal value of 2 kgmol/m³. To do so, the controller must reject both measured and unmeasured disturbances.

In the Scenario section, click Edit Scenario > scenario1.

In the Simulation Scenario dialog box, in the **Reference Signals** table, in the **Signal** drop-down list select **Constant** to hold the output setpoint at its nominal value.

In the Measured Disturbances table, in the Signal drop-down list, select Step.

Specify a step **Size** of 10 and a step **Time** of 0.

	Settings					
Plant	used in simu	lation: Defau	lt (controller in	ternal mode	el)	-
Simulation	n duration (se	conds) 10				
🗖 Run o	pen-loop simula	ation	Use unconst	rained MPC		
Previe	w references	(look ahead)	Preview mea	sured distur	rbances (look al	head)
Reference	Signals (setp	oints for all o	utputs)			
<u> </u>	Name	Nominal	Signal	Size	Time	Period
Channel			1 -	1		
r(1)	Ref of CA	2	Constant			
r(1)		2 (inputs to ME	b	-		
r(1)			b	Size	Time	Period
r(1) Measured [Disturbances	(inputs to ME) channels) Signal		Time	Period

Click OK.

In the **Data Browser**, under **Scenarios**, double-click scenario1 and rename it MD_reject.

In the **Scenario** section, click **Plot Scenario** > **New Scenario**.

In the Simulation Scenario dialog box, in the **Unmeasured Disturbances** table, in the **Signal** drop-down list, select **Step**.

Specify a step Size of 1 and a step Time of 0.

Channel	Name	Nominal	Signal	Size	Time	Period
ı(3)	CAi	0	Step	v 1	0	

Click OK.

In the **Data Browser**, under **Scenarios**, double-click NewScenario and rename it UD_reject.

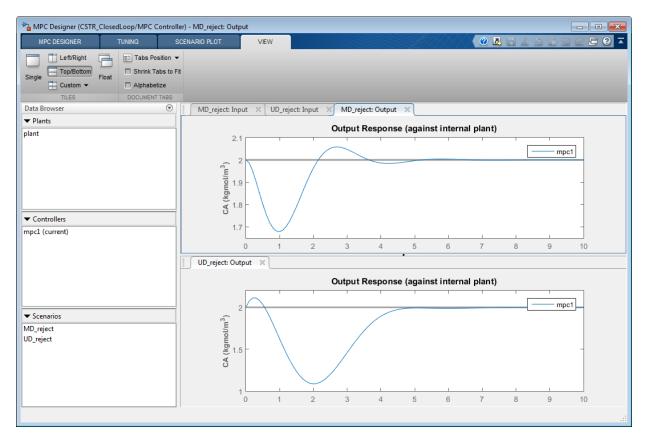
Arrange Output Response Plots

To make viewing the tuning results easier, arrange the plot area to display the Output Response plots for both scenarios at the same time.

On the **View** tab, in the **Tiles** section, click **Top/Bottom**.

The plot display area changes to display the Input Response plots above the Output Response plots.

Drag the **MD_reject: Output** tab up to the top plot.



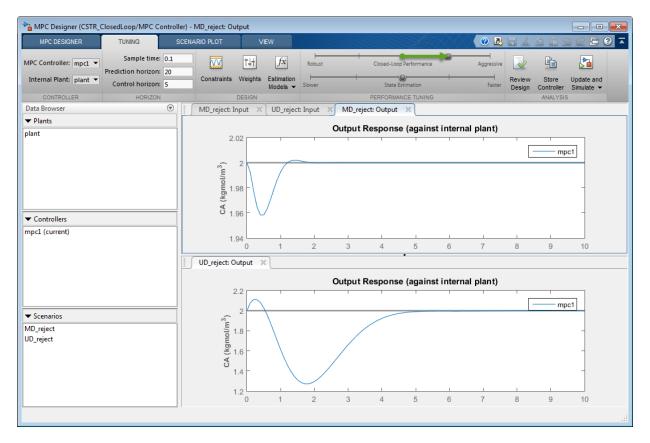
Tune Controller Performance

In the **Tuning** tab, in the **Horizon** section, specify a **Prediction horizon** of 20 and a **Control horizon** of 5.

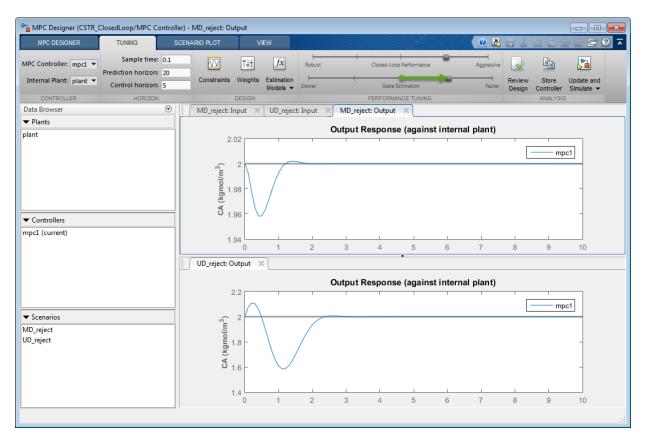
The **Output Response** plots update based on the new horizon values.

Use the default controller constraint and weight configurations.

In the **Performance Tuning** section, drag the **Closed-Loop Performance** slider to the right, which leads to tighter control of outputs and more aggressive control moves. Drag the slider until the **MD_reject: Output** response reaches steady state in less than 2 seconds.



Drag the **State Estimation** slider to the right, which leads to more aggressive unmeasured disturbance rejection. Drag the slider until the **UD_reject: Output** response reaches steady state in less than 3 seconds.



Update Simulink Model with Tuned Controller

In the Analysis section, click the Update and Simulate arrow **v**.

Under **Update and Simulate**, click **Update Block Only**. The app exports the tuned controller, mpc1, to the MATLAB workspace. In the Simulink model, the MPC Controller block is updated to use the exported controller.

Simulate Unmeasured Disturbance Rejection

In the Simulink model window, change the simulation duration to 5 seconds.

🔁 CSTR_C	losedLoo	p * - Simuli	nk									
File Edit	View	Display	Diagram	Simulation	Analysis	Code	Tools	Help				
🔁 - E		\$ €	<u>2</u> • • • •) • 📰 •	r 🖗	▶		2	5	>	» 🕢 🔻	**** ~
CSTR_Clos	edLoop											
🛞 🎦 CS	TR_Close	dLoop 🕨										•
<u>.</u>						_		_			_	

The model initial conditions are set to the nominal operating point used for linearization.

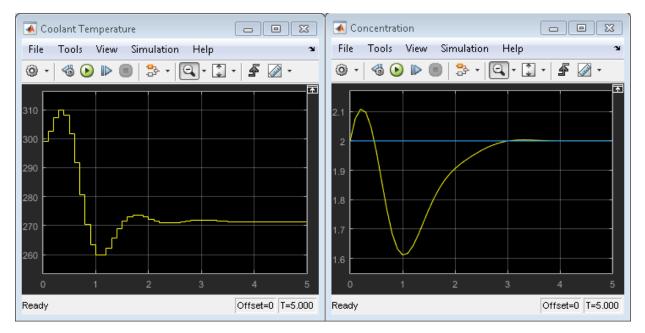
Double-click the Feed Concentration block.

In the Block Parameters dialog box, enter a ${\bf Constant}$ ${\bf Value}$ of 11 to simulate a unit step at time zero.

🔁 Block Parameters: Feed Concentration
Constant
Output the constant specified by the 'Constant value' parameter. If 'Constant value' is a vector and 'Interpret vector parameters as 1-D' is on, treat the constant value as a 1-D array. Otherwise, output a matrix with the same dimensions as the constant value.
Main Signal Attributes
Constant value:
11
Interpret vector parameters as 1-D
Sample time:
0
OK Cancel Help Apply

Click Apply.

In the Simulink model window, click **Run**.



The **Concentration** output response is similar to the **UD_reject** response, however the settling time is around 1 second later. The different result is due to the mismatch between the linear plant used in the **MPC Designer** simulation and the nonlinear plant in the Simulink model.

Simulate Measured Disturbance Rejection

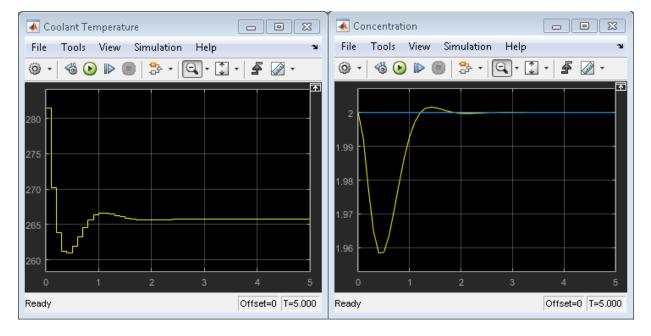
In the Block Parameters: Feed Concentration dialog box, enter a **Constant Value** of 10 to return the feed concentration to its nominal value.

Click OK.

In the Simulink model window, double-click the Feed Temperature block.

In the Block Parameters: Feed Temperature dialog box, enter a **Constant Value** of **310** to simulate a step change of size 10 at time zero.

Click OK.



In the Simulink model window, click **Run**.

The **Concentration** output response is similar to the **MD_reject** response from the **MPC Designer** simulation.

References

[1] Seborg, D. E., T. F. Edgar, and D. A. Mellichamp, Process Dynamics and Control, 2nd Edition, Wiley, 2004, pp. 34-36 and 94-95.

See Also

MPC Controller | MPC Designer

More About

- "Tune Weights"
- "Linearize Simulink Models" on page 2-22

•

"Design Controller Using MPC Designer" on page 3-2

Control of a Single-Input-Single-Output Plant

This example shows how to control a double integrator plant under input saturation in Simulink $\ensuremath{\mathbb{B}}$.

Define Plant Model

The linear open-loop dynamic model is a double integrator:

plant = tf(1,[1 0 0]);

Design MPC Controller

Create the controller object with sampling period, prediction and control horizons:

```
Ts = 0.1;
p = 10;
m = 3;
mpcobj = mpc(plant, Ts, p, m);
```

```
-->The "Weights.ManipulatedVariables" property of "mpc" object is empty. Assuming defau
-->The "Weights.ManipulatedVariablesRate" property of "mpc" object is empty. Assuming default 1
-->The "Weights.OutputVariables" property of "mpc" object is empty. Assuming default 1
```

Specify actuator saturation limits as MV constraints.

mpcobj.MV = struct('Min',-1,'Max',1);

Simulate Using Simulink®

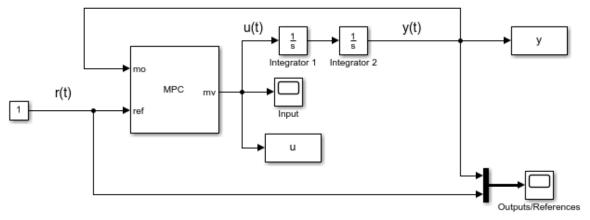
To run this example, Simulink® is required.

```
if ~mpcchecktoolboxinstalled('simulink')
    disp('Simulink(R) is required to run this example.')
    return
end
```

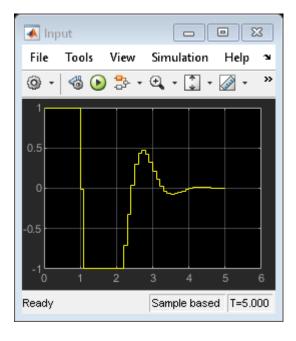
Simulate closed-loop control of the linear plant model in Simulink. Controller "mpcobj" is specified in the block dialog.

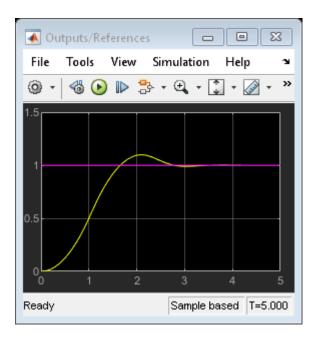
```
mdl = 'mpc_doubleint';
open_system(mdl);
sim(mdl);
-->Converting the "Model.Plant" property of "mpc" object to state-space.
-->Converting model to discrete time.
```

Assuming no disturbance added to measured output channel #1. -->The "Model.Noise" property of the "mpc" object is empty. Assuming white noise on ear



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The closed-loop response shows good setpoint tracking performance.

bdclose(mdl)

See Also

MPC Controller | MPC Designer | mpc

More About

- "Control of a Multi-Input Single-Output Plant" on page 3-62
- "Control of a Multi-Input Multi-Output Nonlinear Plant" on page 3-96

Control of a Multi-Input Single-Output Plant

This example shows how to design model predictive controller with one measured output, one manipulated variable, one measured disturbance, and one unmeasured disturbance in a typical workflow.

Define Plant Model

The discrete time linear open-loop dynamic model is defined below with sample time Ts.

sys = ss(tf({1,1,1}, {[1 .5 1], [1 1], [.7 .5 1]})); Ts = 0.2; model = c2d(sys,Ts);

Design MPC Controller

Define type of input signals: the first signal is a manipulated variable, the second signal is a measured disturbance, the third one is an unmeasured disturbance.

```
model = setmpcsignals(model, 'MV', 1, 'MD', 2, 'UD', 3);
```

Create the controller object with sampling period, prediction and control horizons.

```
mpcobj = mpc(model,Ts,10,3);
```

```
-->The "Weights.ManipulatedVariables" property of "mpc" object is empty. Assuming defau-->The "Weights.ManipulatedVariablesRate" property of "mpc" object is empty. Assuming default 1 ->The "Weights.OutputVariables" property of "mpc" object is empty. Assuming default 1
```

Define constraints on the manipulated variable.

```
mpcobj.MV = struct('Min',0,'Max',1,'RateMin',-10,'RateMax',10);
```

For unmeasured input disturbances, its model is an integrator driven by white noise with variance = 1000.

```
mpcobj.Model.Disturbance = tf(sqrt(1000),[1 0]);
```

Simulate Closed-Loop Response Using the sim Command

Specify simulation parameters.

Tstop = 30;	%	simulat	ior	n time	
<pre>Tf = round(Tstop/Ts);</pre>	%	number	of	simulation	steps

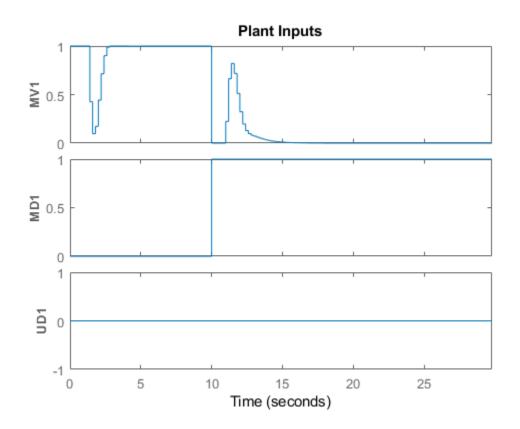
r	=	ones(Tf,1);
v	=	<pre>[zeros(Tf/3,1);ones(2*Tf/3,1)];</pre>

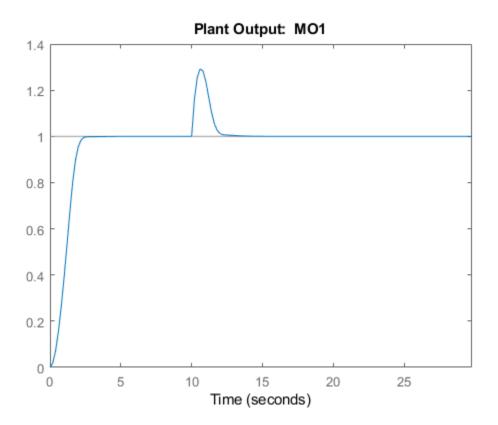
% reference signal % measured disturbance signal

Run the closed-loop simulation and plot results.

sim(mpcobj,Tf,r,v)

Assuming no disturbance added to measured output channel #1. -->The "Model.Noise" property of the "mpc" object is empty. Assuming white noise on ear





Specify disturbance and noise signals in simulation option object.

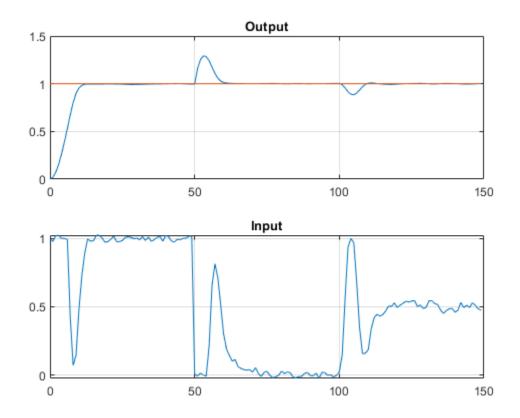
% unmeasured input disturbance signal % output measurement noise % noise on manipulated variables

Run the closed-loop simulation and save the results to the workspace.

[y,t,u,xp] = sim(mpcobj,Tf,r,v,SimOptions);

Plot results.

```
figure
subplot(2,1,1)
plot(0:Tf-1,y,0:Tf-1,r)
title('Output')
grid
subplot(2,1,2)
plot(0:Tf-1,u)
title('Input')
grid
```



Simulate Closed-Loop Response with Model Mismatch

Test the robustness of the MPC controller against a model mismatch. Specify the true plant simModel, with a nominal output value of 0.1.

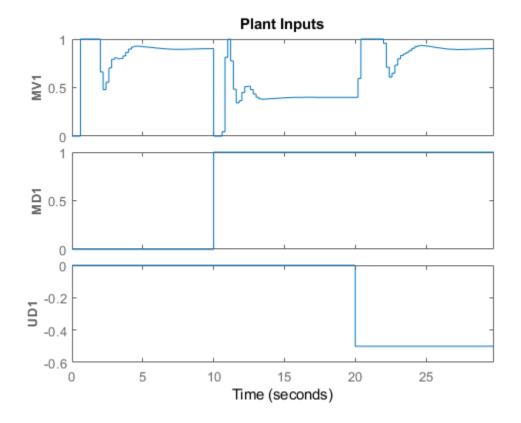
```
simModel = ss(tf({1,1,1},{[1 .8 1],[1 2],[.6 .6 1]}));
simModel = setmpcsignals(simModel,'MV',1,'MD',2,'UD',3);
simModel = struct('Plant',simModel);
simModel.Nominal.Y = 0.1;
simModel.Nominal.X = -.1*[1 1 1 1];
```

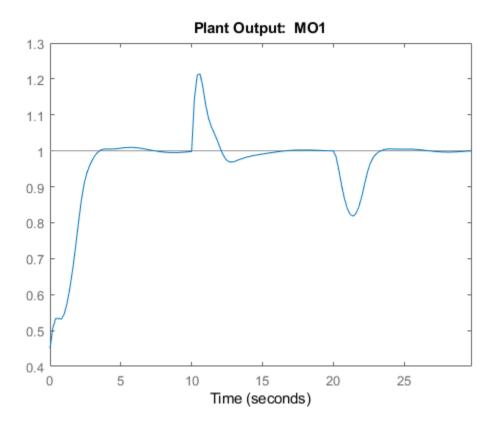
Create option object.

```
SimOptions.Model = simModel;
SimOptions.plantinit = [0.1 0 -0.1 0 .05]; % Initial state of the true plant
SimOptions.OutputNoise = []; % remove output measurement noise
SimOptions.InputNoise = []; % remove noise on manipulated variables
```

% Run the closed-loop simulation and plot results. sim(mpcobj,Tf,r,v,SimOptions)

-->Converting model to discrete time.





Soften Constraints

Relax the constraints on manipulated variables from hard to soft.

mpcobj.MV.MinECR = 1; mpcobj.MV.MaxECR = 1;

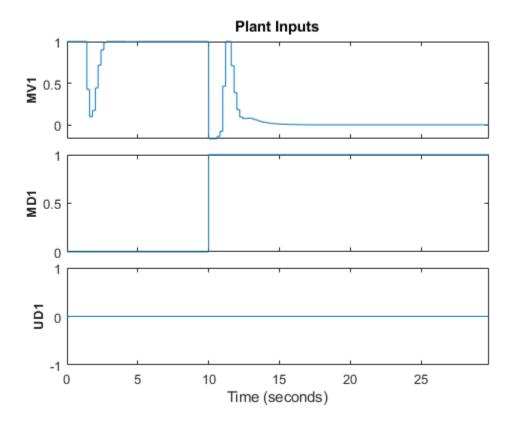
Define an output constraint.

mpcobj.OV.Max = 1.1;

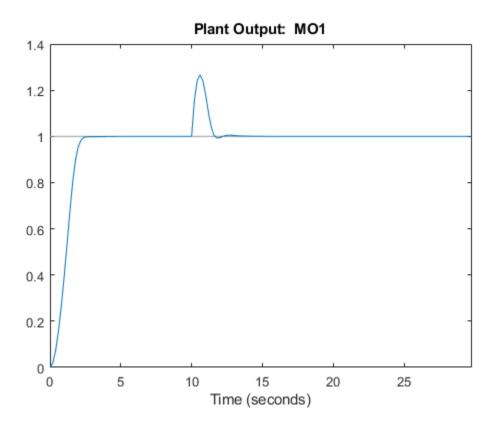
Run a new closed-loop simulation.

sim(mpcobj,Tf,r,v)

Assuming no disturbance added to measured output channel #1. -->The "Model.Noise" property of the "mpc" object is empty. Assuming white noise on ear



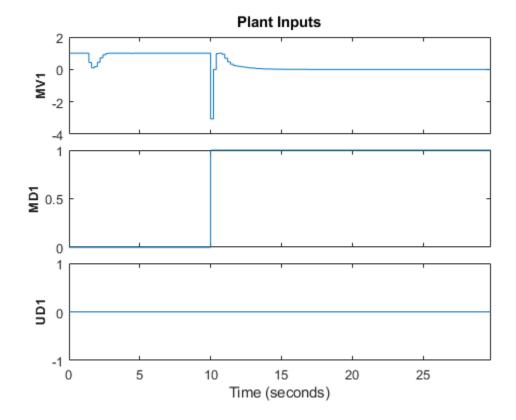
3-69

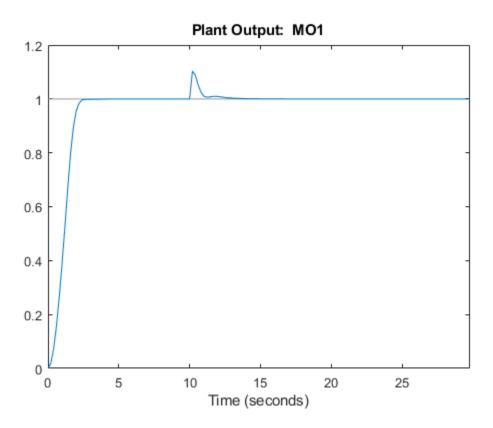


MV constraint has been slightly violated while MO constraint has been violated more. Penalize more output constraint and rerun the simulation.

mpcobj.OV.MaxECR = 0.001; % The closer to zero, the harder the constraint sim(mpcobj,Tf,r,v)

Assuming no disturbance added to measured output channel #1. -->The "Model.Noise" property of the "mpc" object is empty. Assuming white noise on ear





Now MO constraint has been slightly violated while MV constraint has been violated more as expected.

Change Kalman Gains Used in the Built-In State Estimator

Model Predictive Control Toolbox^m software provides a default Kalman filter to estimate the state of plant, disturbance, and noise models. You can change the Kalman gains.

First, retrieve the default Kalman gains and state-space matrices.

[L,M,A1,Cm1] = getEstimator(mpcobj);

The default observer poles are:

e = eig(A1-A1*M*Cm1)

0.5708 + 0.4144i 0.5708 - 0.4144i 0.4967 + 0.0000i 0.9334 + 0.1831i 0.9334 - 0.1831i 0.8189 + 0.0000i

e =

Design a new state estimator by pole-placement.

```
poles = [.8 .75 .7 .85 .6 .81];
L = place(A1',Cm1',poles)';
M = A1\L;
setEstimator(mpcobj,L,M);
```

Simulate Open-Loop Response

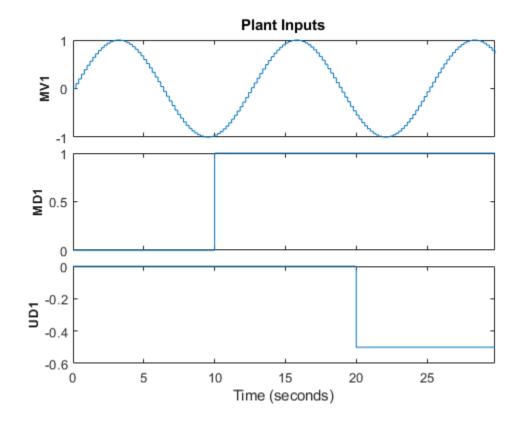
Test the behavior of plant in open-loop using the sim command. Set the OpenLoop flag to on, and provide the sequence of manipulated variables that excite the system.

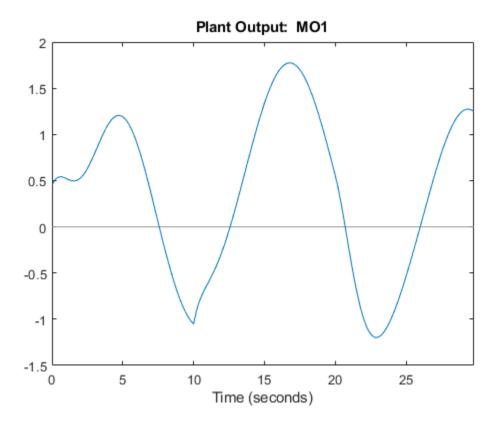
SimOptions.OpenLoop = 'on'; SimOptions.MVSignal = sin((0:Tf-1)'/10);

As the reference signal will be ignored, we can avoid specifying it.

sim(mpcobj,Tf,[],v,SimOptions)

```
Assuming no disturbance added to measured output channel #1.
-->The "Model.Noise" property of the "mpc" object is empty. Assuming white noise on ear
-->Converting model to discrete time.
```





Examine Steady-State Offset

To examine whether the MPC controller will be able to reject constant output disturbances and track constant setpoint with zero offsets in steady-state, compute the DC gain from output disturbances to controlled outputs using the cloffset command.

```
DC = cloffset(mpcobj);
fprintf('DC gain from output disturbance to output = %5.8f (=%g) \n',DC,DC);
DC gain from output disturbance to output = 0.00000000 (=3.10862e-15)
```

A zero gain means that the output will track the desired setpoint.

Simulate MPC with mpcmove

First, obtain the discrete-time state-space matrices of the plant.

```
[A,B,C,D] = ssdata(model);
Tstop = 5; % Simulation time
x = [0 0 0 0 0]'; % Initial state of the plant
xmpc = mpcstate(mpcobj); % Initial state of the MPC controller
r = 1; % Output reference signal
```

Store the closed-loop MPC trajectories in arrays YY, UU, and XX.

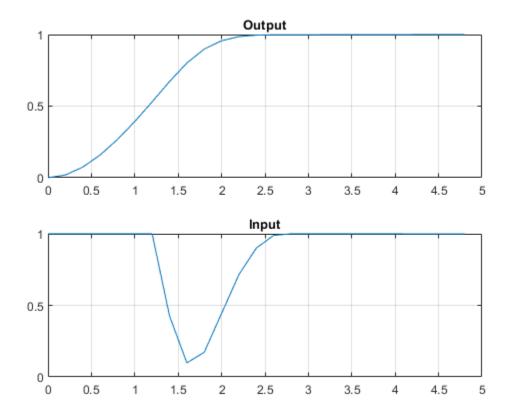
YY=[]; UU=[]; XX=[];

Run the simulation loop

```
for t=0:round(Tstop/Ts)-1
    % Store states
    XX = [XX,x]; %#ok<*AGROW>
    % Define measured disturbance signal
    v = 0;
    if t*Ts>=10
        v = 1;
    end
    % Define unmeasured disturbance signal
    d = 0;
    if t*Ts >= 20
       d = -0.5;
    end
    % Plant equations: output update (no feedthrough from MV to Y)
    y = C*x + D(:,2)*v + D(:,3)*d;
    YY = [YY, y];
    % Compute MPC action
    u = mpcmove(mpcobj,xmpc,y,r,v);
    % Plant equations: state update
    x = A^*x + B(:,1)^*u + B(:,2)^*v + B(:,3)^*d;
    UU = [UU,u];
end
Plot the results.
```

figure
subplot(2,1,1)

```
plot(0:Ts:Tstop-Ts,YY)
grid
title('Output')
subplot(2,1,2)
plot(0:Ts:Tstop-Ts,UU)
grid
title('Input')
```

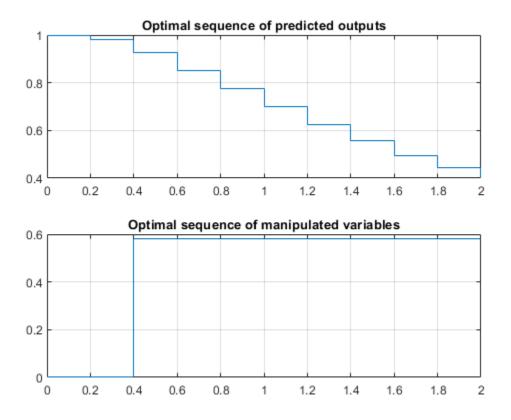


If at any time during the simulation you want to check the optimal predicted trajectories, it can be returned by mpcmove as well. Assume you want to start from the current state and have a set-point change to 0.5, and assume the measured disturbance is gone.

```
r = 0.5;
v = 0;
[~,Info] = mpcmove(mpcobj,xmpc,y,r,v);
```

We now extract the optimal predicted trajectories.

```
topt = Info.Topt;
yopt = Info.Yopt;
uopt = Info.Uopt;
figure
subplot(2,1,1)
stairs(topt,yopt)
title('Optimal sequence of predicted outputs')
grid
subplot(2,1,2)
stairs(topt,uopt)
title('Optimal sequence of manipulated variables')
grid
```



Linear Representation of MPC Controller

When the constraints are not active, MPC controller behaves like a linear controller. You can get the state-space form of the MPC controller.

LTI = ss(mpcobj,'rv');

Get state-space matrices of linearized controller.

[AL,BL,CL,DL] = ssdata(LTI);

Simulate linear MPC closed-loop system and compare the linearized MPC controller with the original MPC controller with constraints turned off.

```
mpcobj.MV = [];
                          % No input constraints
mpcobj.OV = [];
                          % No output constraints
Tstop = 5;
                          %Simulation time
xL = zeros(size(BL,1),1); % Initial state of linearized MPC controller
x = [0 \ 0 \ 0 \ 0 \ 0]';
                          % Initial state of plant
                           % Initial measured output
y = 0;
r = 1;
                           % Output reference set-point
u = 0;
                           % Previous input command
YY = [];
XX = [];
xmpc = mpcstate(mpcobj);
for t = 0:round(Tstop/Ts)-1
    YY = [YY, y];
    XX = [XX, x];
    v = 0;
    if t*Ts>=10
        v = 1;
    end
    d = 0;
    if t*Ts >= 20
        d = -0.5;
    end
    uold = u:
    % Compute the linear MPC control action
    u = CL*xL+DL*[y;r;v];
    % Compare the input move with the one provided by MPCMOVE
    uMPC = mpcmove(mpcobj,xmpc,y,r,v);
    dispStr(t+1) = {sprintf('t=%5.2f, u=%7.4f (provided by LTI), u=%7.4f (provided by I
    % Update plant equations
    x = A^*x + B(:,1)^*u + B(:,2)^*v + B(:,3)^*d;
    % Update controller equations
    xL = AL*xL + BL*[y;r;v];
    % Update output equations
    y = C*x + D(:,1)*u + D(:,2)*v + D(:,3)*d;
end
```

Assuming no disturbance added to measured output channel #1. -->The "Model.Noise" property of the "mpc" object is empty. Assuming white noise on ear

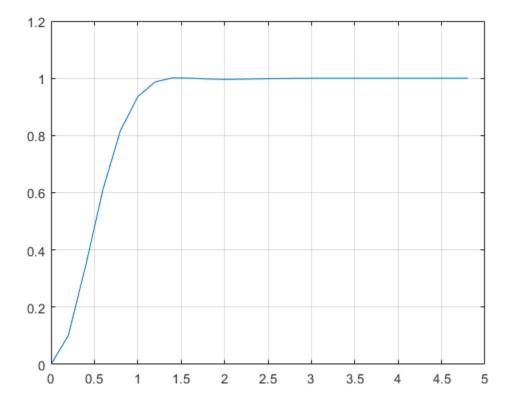
Display the results.

```
for t=0:round(Tstop/Ts)-1
    disp(dispStr{t+1});
end
```

```
t= 0.00, u= 5.2478 (provided by LTI), u= 5.2478 (provided by MPCOBJ)
t= 0.20, u= 3.0134 (provided by LTI), u= 3.0134 (provided by MPCOBJ)
t= 0.40, u= 0.2281 (provided by LTI), u= 0.2281 (provided by MPCOBJ)
t= 0.60, u=-0.9952 (provided by LTI), u=-0.9952 (provided by MPCOBJ)
t= 0.80, u=-0.8749 (provided by LTI), u=-0.8749 (provided by MPCOBJ)
t= 1.00, u=-0.2022 (provided by LTI), u=-0.2022 (provided by MPCOBJ)
t= 1.20, u= 0.4459 (provided by LTI), u= 0.4459 (provided by MPCOBJ)
t= 1.40, u= 0.8489 (provided by LTI), u= 0.8489 (provided by MPCOBJ)
t= 1.60, u= 1.0192 (provided by LTI), u= 1.0192 (provided by MPCOBJ)
t= 1.80, u= 1.0511 (provided by LTI), u= 1.0511 (provided by MPCOBJ)
t= 2.00, u= 1.0304 (provided by LTI), u= 1.0304 (provided by MPCOBJ)
t= 2.20, u= 1.0053 (provided by LTI), u= 1.0053 (provided by MPCOBJ)
t= 2.40, u= 0.9920 (provided by LTI), u= 0.9920 (provided by MPCOBJ)
t= 2.60, u= 0.9896 (provided by LTI), u= 0.9896 (provided by MPCOBJ)
t= 2.80, u= 0.9925 (provided by LTI), u= 0.9925 (provided by MPCOBJ)
t= 3.00, u= 0.9964 (provided by LTI), u= 0.9964 (provided by MPCOBJ)
t= 3.20, u= 0.9990 (provided by LTI), u= 0.9990 (provided by MPCOBJ)
t= 3.40, u= 1.0002 (provided by LTI), u= 1.0002 (provided by MPCOBJ)
t= 3.60, u= 1.0004 (provided by LTI), u= 1.0004 (provided by MPCOBJ)
t= 3.80, u= 1.0003 (provided by LTI), u= 1.0003 (provided by MPCOBJ)
t= 4.00, u= 1.0001 (provided by LTI), u= 1.0001 (provided by MPCOBJ)
t= 4.20, u= 1.0000 (provided by LTI), u= 1.0000 (provided by MPCOBJ)
t= 4.40, u= 0.9999 (provided by LTI), u= 0.9999 (provided by MPCOBJ)
t= 4.60, u= 1.0000 (provided by LTI), u= 1.0000 (provided by MPCOBJ)
t= 4.80, u= 1.0000 (provided by LTI), u= 1.0000 (provided by MPCOBJ)
```

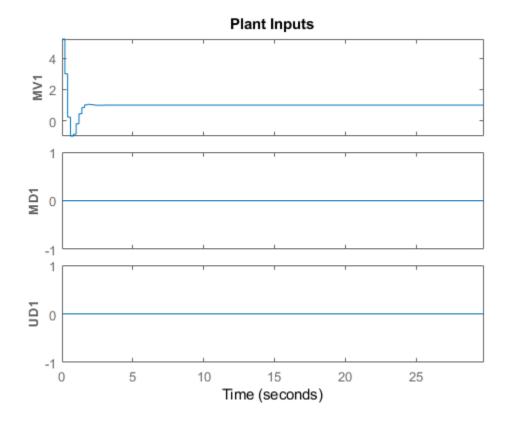
Plot the results.

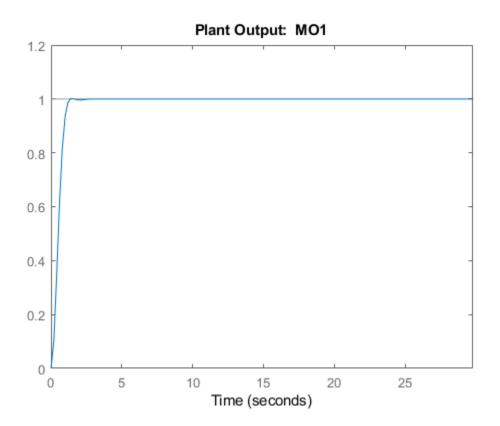
figure
plot(0:Ts:Tstop-Ts,YY)
grid



Running a closed-loop where all constraints are turned off is easy using sim. We just specify an option in the SimOptions structure:

SimOptions = mpcsimopt(mpcobj); SimOptions.Constr = 'off'; % Remove all MPC constraints SimOptions.Unmeas = d; % unmeasured input disturbance sim(mpcobj,Tf,r,v,SimOptions);





Simulate Using Simulink®

To run this example, Simulink® is required.

```
if ~mpcchecktoolboxinstalled('simulink')
    disp('Simulink(R) is required to run this part of the example.')
    return
end
```

Recreate the MPC controller.

```
mpcobj = mpc(model,Ts,10,3);
mpcobj.MV = struct('Min',0,'Max',1,'RateMin',-10,'RateMax',10);
mpcobj.Model.Disturbance = tf(sqrt(1000),[1 0]);
```

-->The "Weights.ManipulatedVariables" property of "mpc" object is empty. Assuming defau -->The "Weights.ManipulatedVariablesRate" property of "mpc" object is empty. Assuming default 1 -->The "Weights.OutputVariables" property of "mpc" object is empty. Assuming default 1

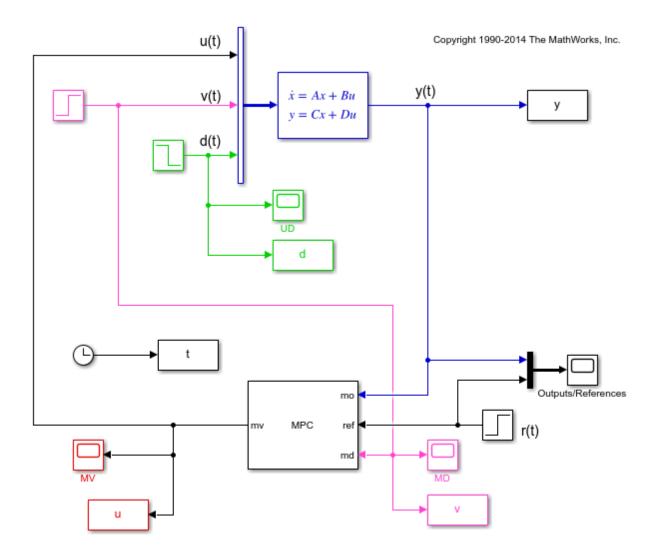
The continuous-time plant to be controlled has the following state-space realization:

[A,B,C,D] = ssdata(sys);

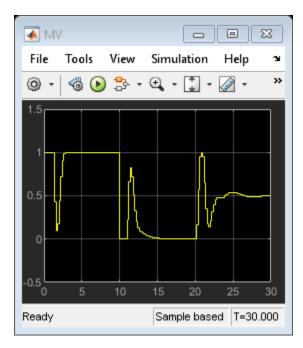
Simulate closed-loop MPC in Simulink.

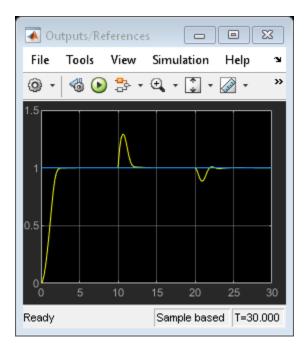
```
mdl1 = 'mpc_miso';
open_system(mdl1)
sim(mdl1)
```

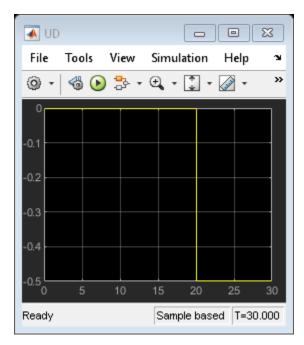
Assuming no disturbance added to measured output channel #1. -->The "Model.Noise" property of the "mpc" object is empty. Assuming white noise on ear



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Next, run a simulation with sinusoidal output noise. Assume output measurements are affected by a sinusoidal measurement noise of frequency 0.1 Hz. You want to inform the MPC object about this so that state estimates can be improved.

```
omega = 2*pi/10;
mpcobj.Model.Noise = 0.5*tf(omega^2,[1 0 omega^2]);
```

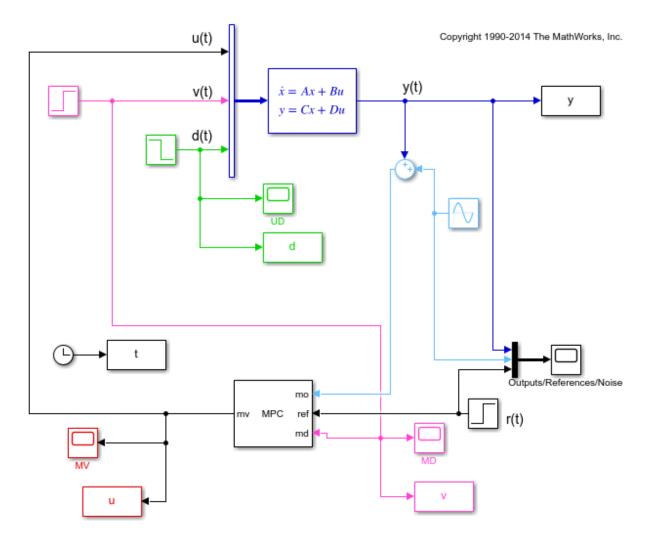
Revise the MPC design and specify a white Gaussian noise unmeasured disturbance with zero mean and variance 0.1.

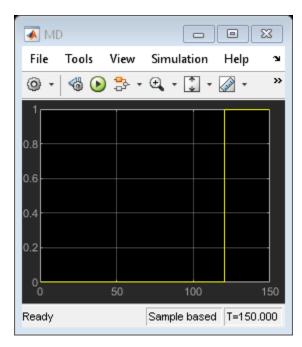
```
mpcobj.Model.Disturbance = tf(0.1);
mpcobj.weights = struct('MV',0,'MVRate',0.1,'0V',0.005);
mpcobj.predictionhorizon = 40;
mpcobj.controlhorizon = 3;
```

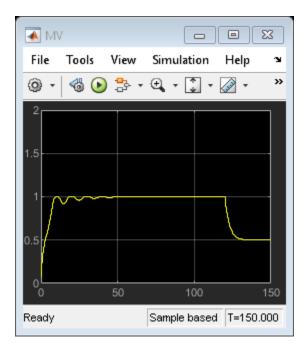
Run the simulation.

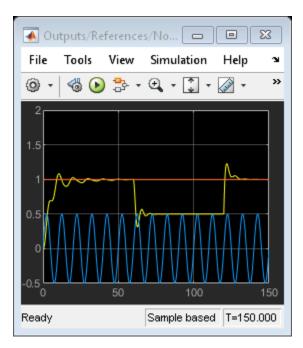
```
Tstop = 150;
mdl2 = 'mpc_misonoise';
open_system(mdl2)
sim(mdl2,Tstop)
```

-->Assuming output disturbance added to measured output channel #1 is integrated white -->A feedthrough channel in NoiseModel was inserted to prevent problems with estimator









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bdclose(mdl1)
bdclose(mdl2)

See Also

MPC Controller | MPC Designer | mpc

More About

- "Control of a Single-Input-Single-Output Plant" on page 3-59
- "Control of a Multi-Input Multi-Output Nonlinear Plant" on page 3-96

Control of a Multi-Input Multi-Output Nonlinear Plant

This example shows how to design a model predictive controller for a multi-input multioutput nonlinear plant. The plant has 3 manipulated variables and 2 measured outputs.

Linearize Nonlinear Plant

To run this example, Simulink® and Simulink Control Design® are required.

```
if ~mpcchecktoolboxinstalled('simulink')
    disp('Simulink(R) is required to run this example.')
    return
end
if ~mpcchecktoolboxinstalled('slcontrol')
    disp('Simulink Control Design(R) is required to run this example.')
    return
end
```

The nonlinear plant is implemented in Simulink® model "mpc_nonlinmodel" and linearized at the default operating condition using the "linearize" command from Simulink Control Design®.

```
plant = linearize('mpc_nonlinmodel');
```

Assign names to I/O variables.

```
plant.InputName = {'Mass Flow';'Heat Flow';'Pressure'};
plant.OutputName = {'Temperature';'Level'};
plant.InputUnit = {'kg/s' 'J/s' 'Pa'};
plant.OutputUnit = {'K' 'm'};
```

Design MPC Controller

Create the controller object with sampling period, prediction and control horizons:

```
Ts = 0.2;
p = 5;
m = 2;
mpcobj = mpc(plant,Ts,p,m);
-->The "Weights.ManipulatedVariables" property of "mpc" object is empty. Assuming defau
-->The "Weights.ManipulatedVariablesRate" property of "mpc" object is empty. Assuming default 1
```

Specify MV constraints.

mpcobj.MV = struct('Min', {-3; -2; -2}, 'Max', {3;2;2}, 'RateMin', {-1000; -1000; -1000});

Define weights on manipulated and controlled variables.

mpcobj.Weights = struct('MV',[0 0 0],'MVRate',[.1 .1 .1],'0V',[1 1]);

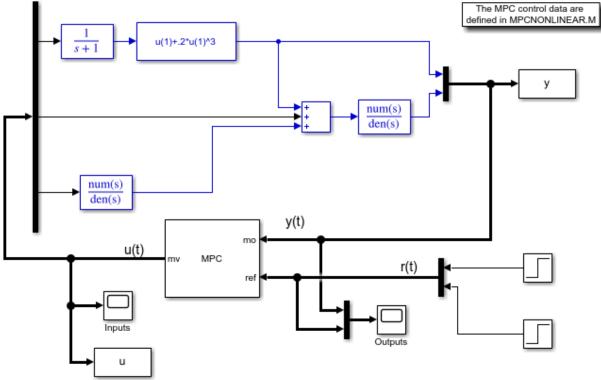
Simulate Using Simulink®

Run simulation.

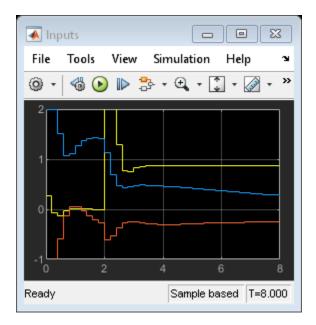
```
mdl1 = 'mpc_nonlinear';
open_system(mdl1) % Open Simulink Model
sim(mdl1); % Start Simulation
```

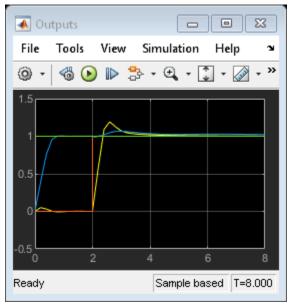
-->Converting model to discrete time.

-->Assuming output disturbance added to measured output channel #1 is integrated white -->Assuming output disturbance added to measured output channel #2 is integrated white -->The "Model.Noise" property of the "mpc" object is empty. Assuming white noise on ear



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Modify MPC Design to Track Ramp Signals

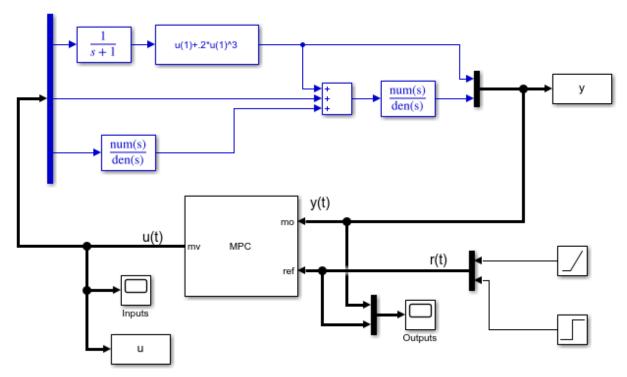
In order to track a ramp, a triple integrator is defined as an output disturbance model on both outputs.

```
outdistmodel = tf({1 0;0 1},{[1 0 0 0],1;1,[1 0 0 0]});
setoutdist(mpcobj,'model',outdistmodel);
```

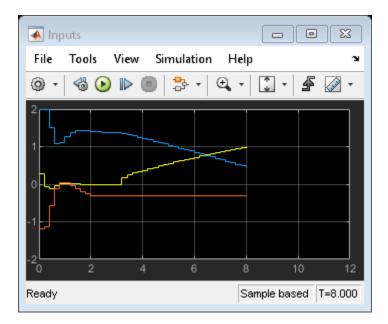
Run simulation.

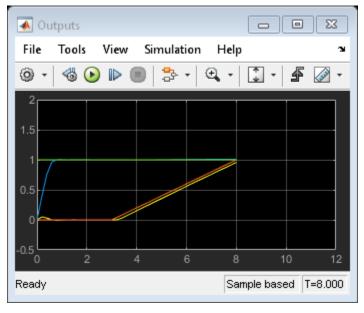
```
mdl2 = 'mpc_nonlinear_setoutdist';
open_system(mdl2) % Open Simulink Model
sim(mdl2); % Start Simulation
```

-->Converting model to discrete time. -->The "Model.Noise" property of the "mpc" object is empty. Assuming white noise on ear



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Simulate without Constraints

When the constraints are not active, the MPC controller behaves like a linear controller.

```
mpcobj.MV = [];
```

Reset output disturbance model to default

```
setoutdist(mpcobj,'integrators');
```

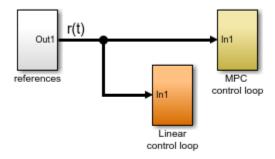
The input to the linear controller LTI is the vector [ym;r], where ym is the vector of measured outputs, and r is the vector of output references.

```
LTI = ss(mpcobj,'r');
```

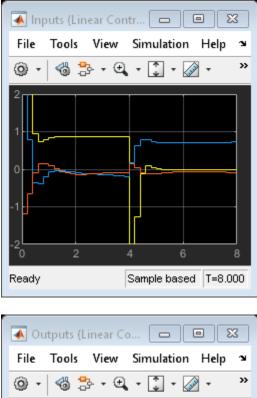
```
-->Converting model to discrete time.
-->Assuming output disturbance added to measured output channel #1 is integrated white
-->Assuming output disturbance added to measured output channel #2 is integrated white
-->The "Model.Noise" property of the "mpc" object is empty. Assuming white noise on eac
```

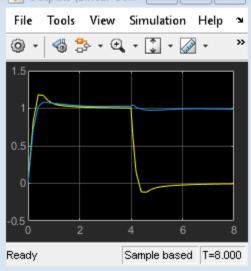
Run simulation.

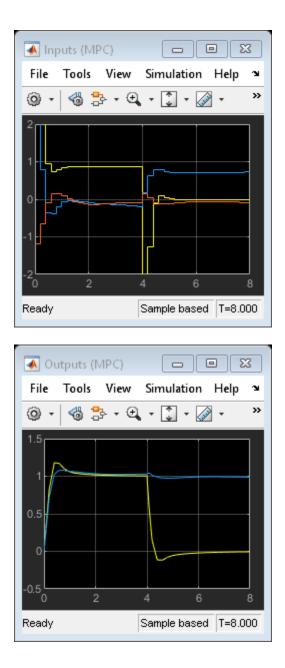
```
refs = [1;1]; % output references are step signals
mdl3 = 'mpc_nonlinear_ss';
open_system(mdl3) % Open Simulink(R) Model
sim(mdl3); % Start Simulation
```



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Compare Simulation Results

```
fprintf('Compare output trajectories: ||ympc-ylin|| = %g\n',norm(ympc-ylin));
disp('The MPC controller and the linear controller produce the same closed-loop traject
Compare output trajectories: ||ympc-ylin|| = 1.50163e-14
The MPC controller and the linear controller produce the same closed-loop trajectories
bdclose(mdl1)
bdclose(mdl2)
bdclose(mdl3)
```

See Also

MPC Controller | MPC Designer | mpc

More About

- "Control of a Single-Input-Single-Output Plant" on page 3-59
- "Control of a Multi-Input Single-Output Plant" on page 3-62